

Experimentalist's view on

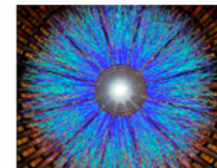
# Fluctuations

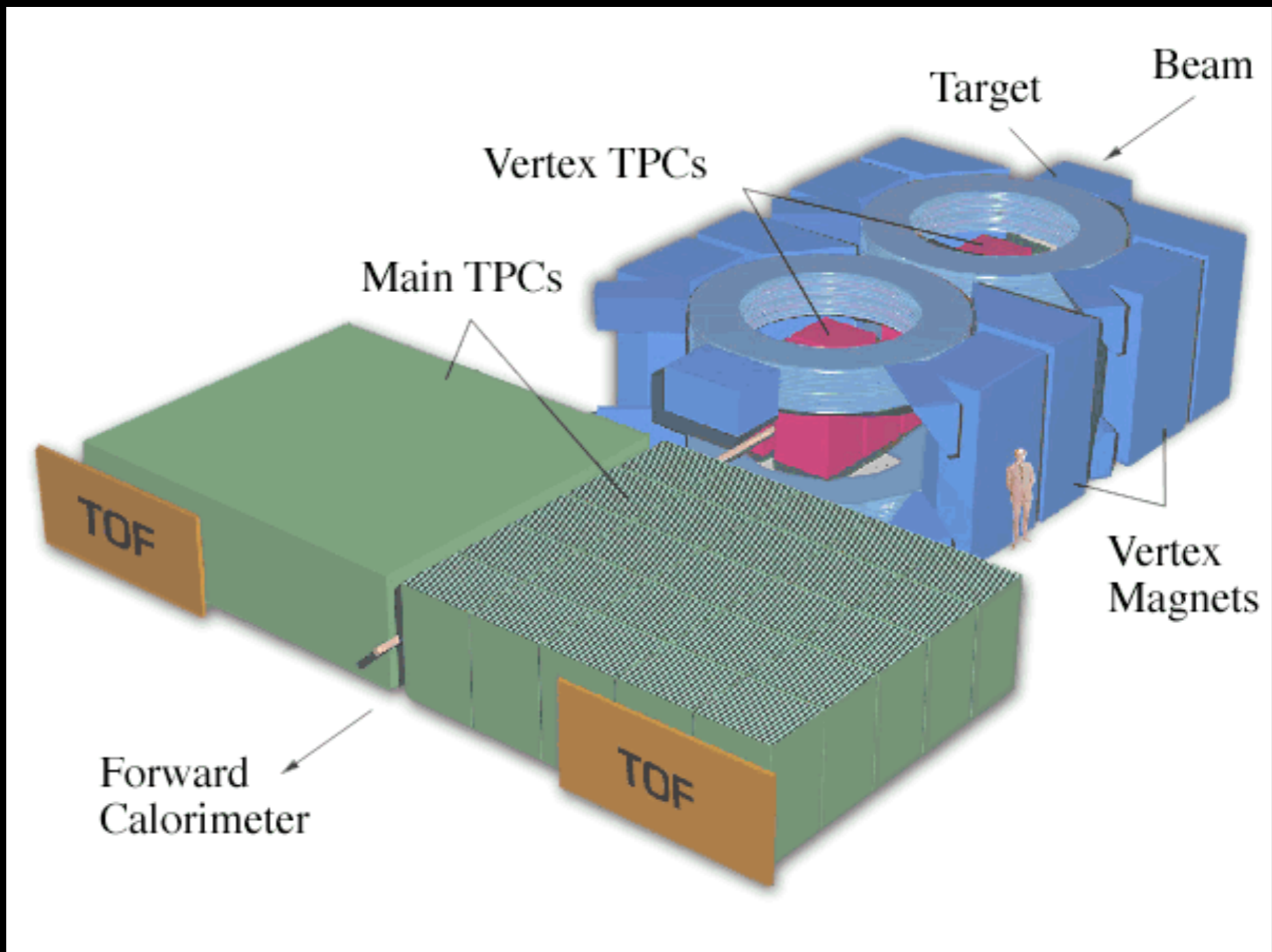
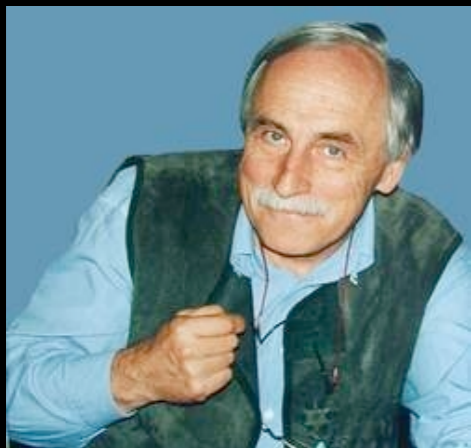
(and correlations)

Gunther Roland



**School of Collective Dynamics in High Energy Collisions**  
June 7 - 11, 2010

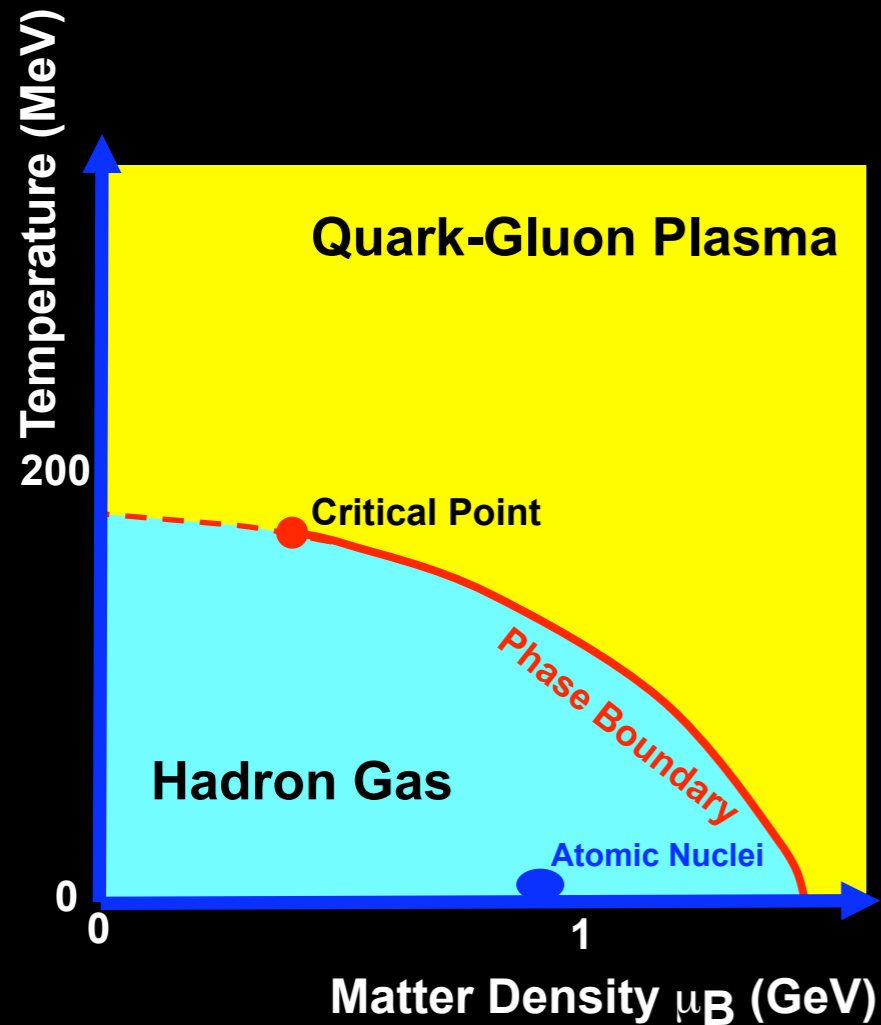




1994: Start of event-by-event fluctuation program



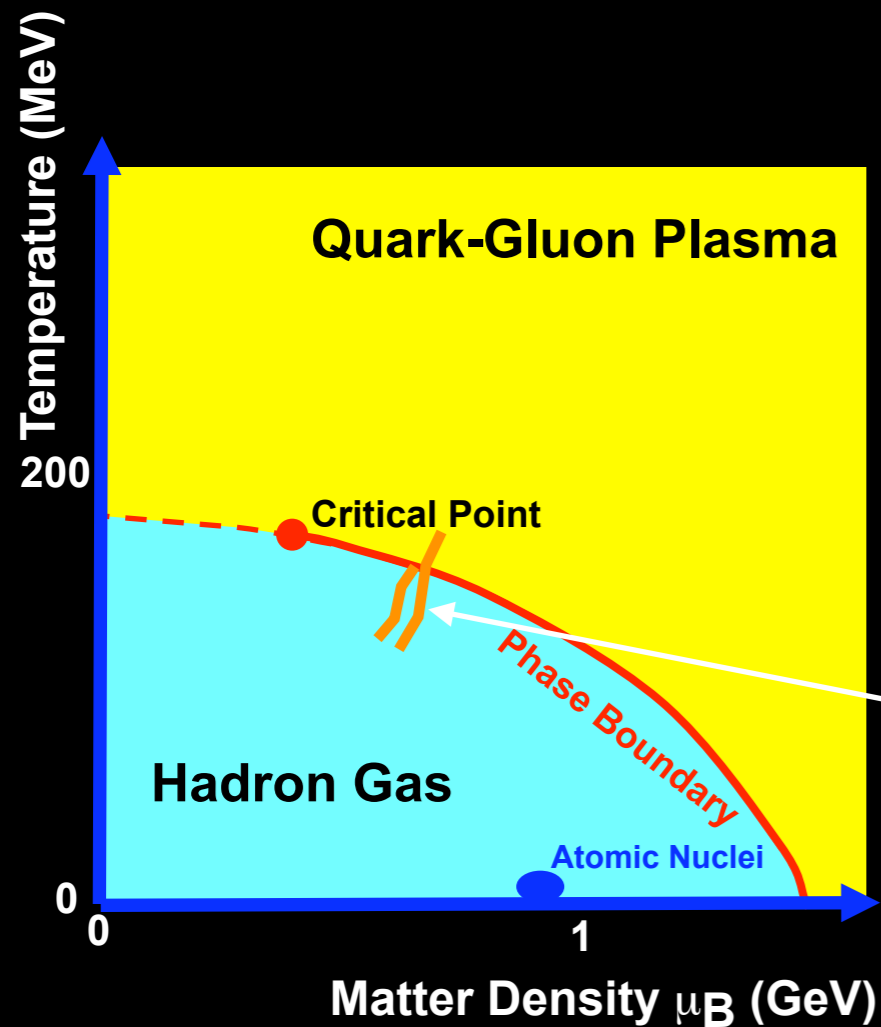
# Exploring the QCD Phase Diagram



What is the nature of the phase transition?

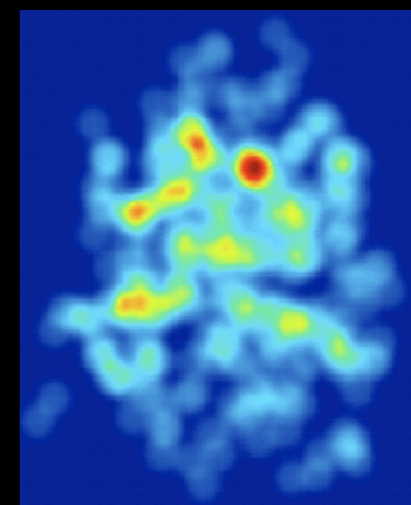
Is there a critical point (and where is it)?

What are the properties of matter at high T?



R. Stock: Even at fixed  $(\sqrt{s}, b)$   
not all collisions created equal:  
Study collisions event-by-event

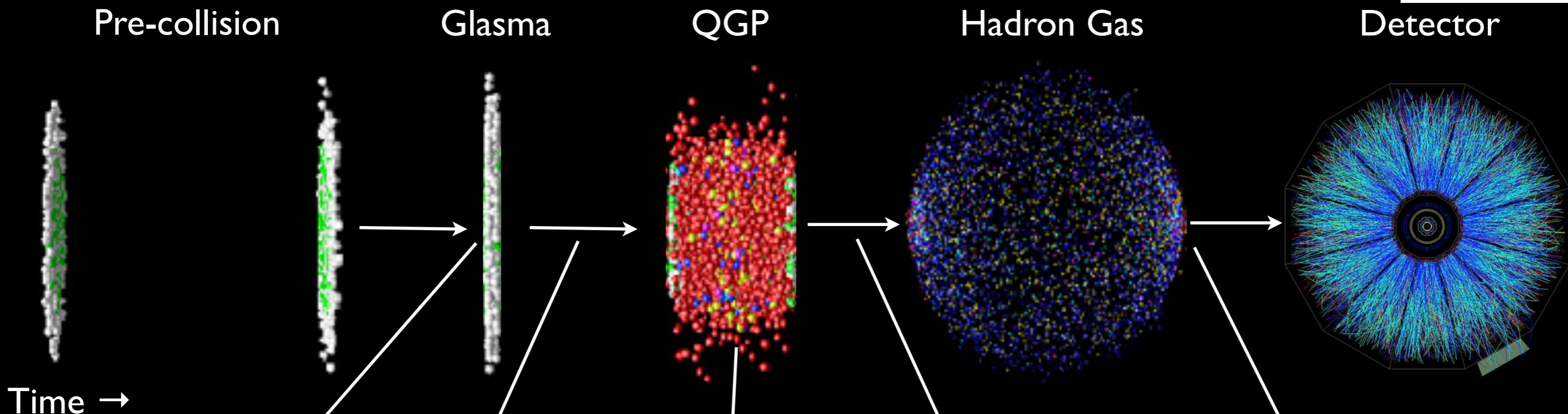
Density of collision points  
in a single AuAu event  
(Glauber MC/Mike McCumber)



Collision of two finite systems:

Energy density variation from event to event

Energy density variation within the event



**Initial collisions**

**Equilibration**

**Hydrodynamic expansion**

**Phase transition**

**Hadronic rescattering**

Energy density & geometry fluctuations;  
Glasma flux tubes;  
jets

Fluctuations of conserved quantum numbers

Critical fluctuations; supercooling/bubble formation; cluster formation

Bose-Einstein correlations; resonance decays



# Many potential sources of fluctuations

## How are fluctuations modified during system evolution?

### Can they be seen/distinguished experimentally?

Initial collisions

Equilibration

Hydrodynamic expansion

Phase transition

Hadronic rescattering

Energy density & geometry fluctuations;  
Glasma flux tubes;  
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Critical fluctuations;  
supercooling/bubble formation;  
cluster formation

Bose-Einstein correlations;  
resonance decays

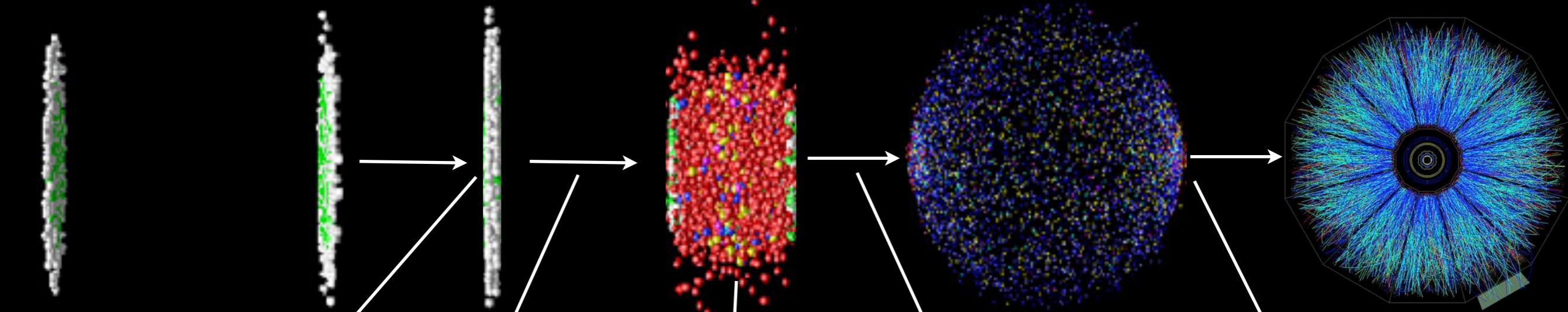
Pre-collision

Glasma

QGP

Hadron Gas

Detector



Initial collisions

Equilibration

Hydrodynamic expansion

Phase transition

Hadronic rescattering

Energy density & geometry fluctuations; Glasma flux tubes; jets

Fluctuations of conserved quantum numbers

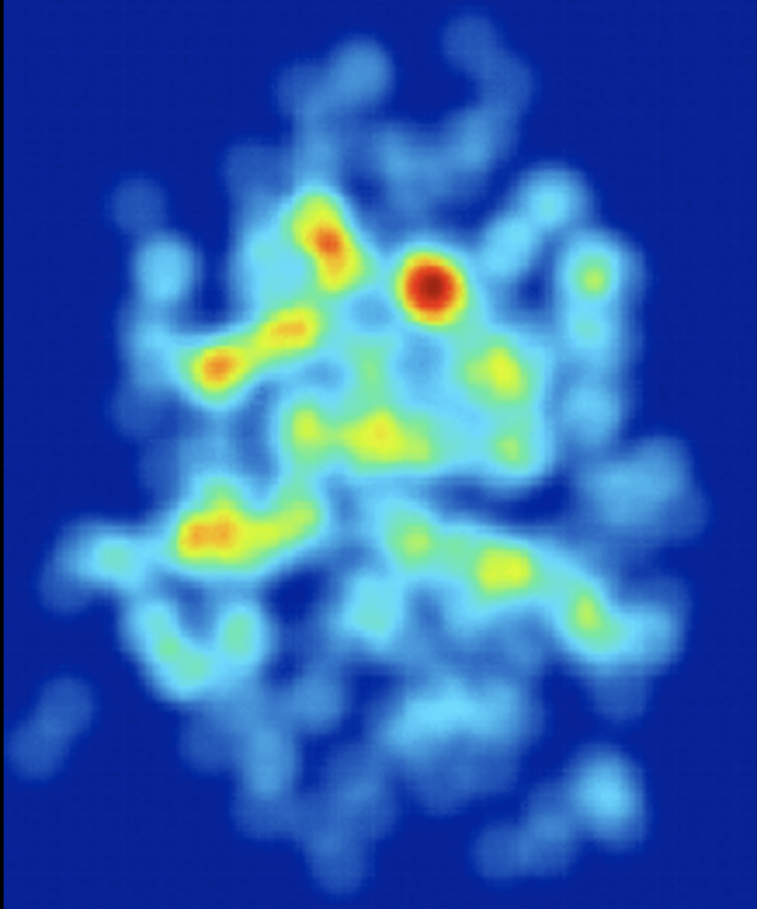
Critical fluctuations; supercooling/bubble formation; cluster formation

Bose-Einstein correlations; resonance decays

Glasma



Initial collisions

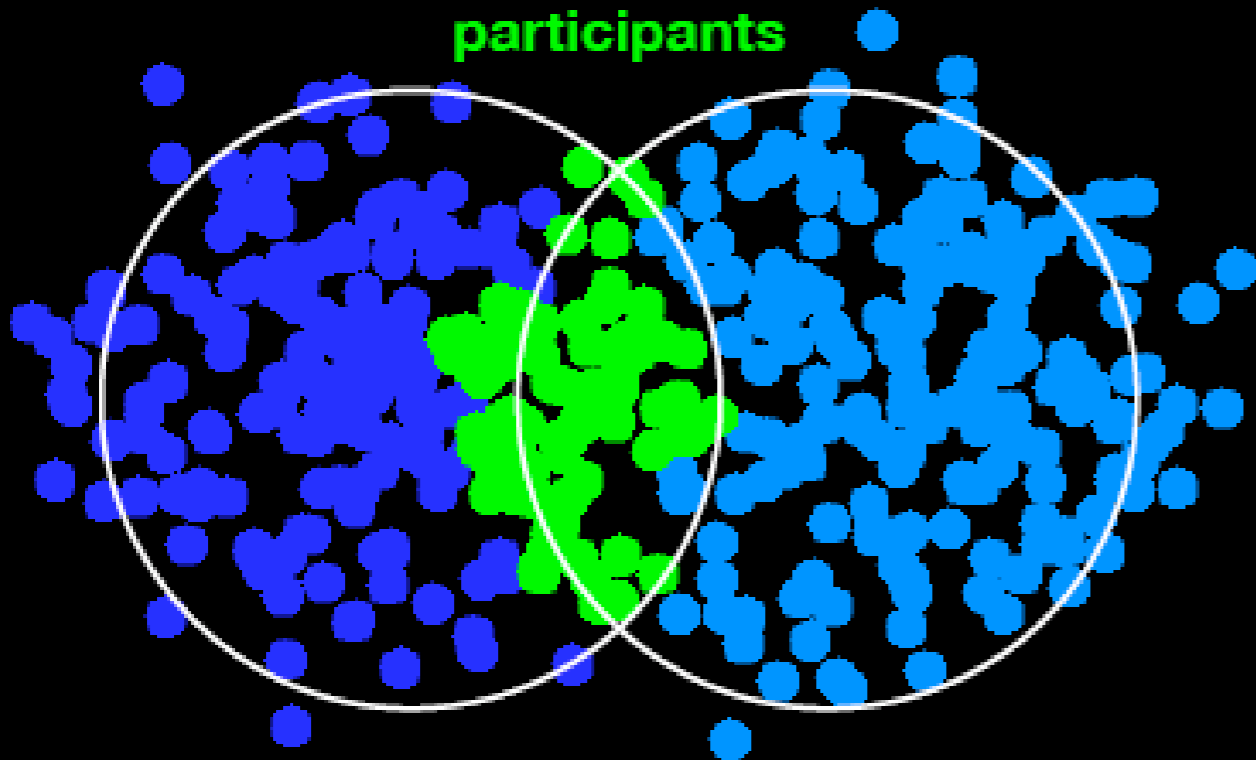


Energy density & geometry fluctuations;  
Glasma flux tubes;  
jets



At fixed  $b$

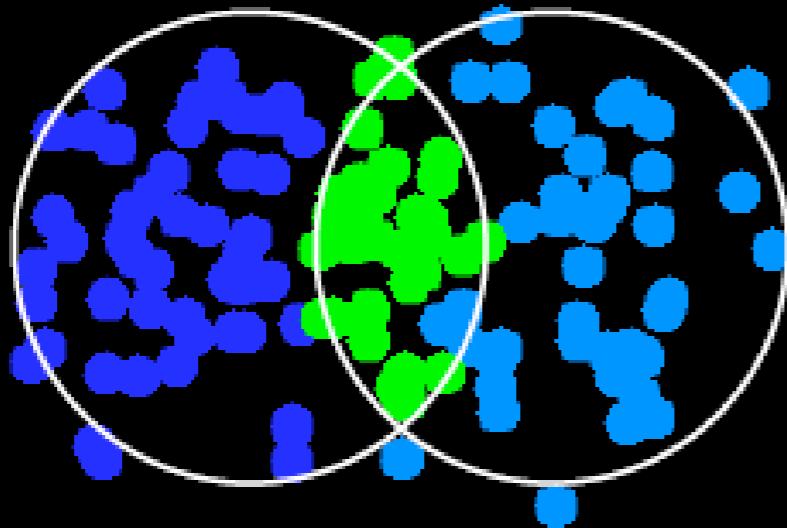
participants



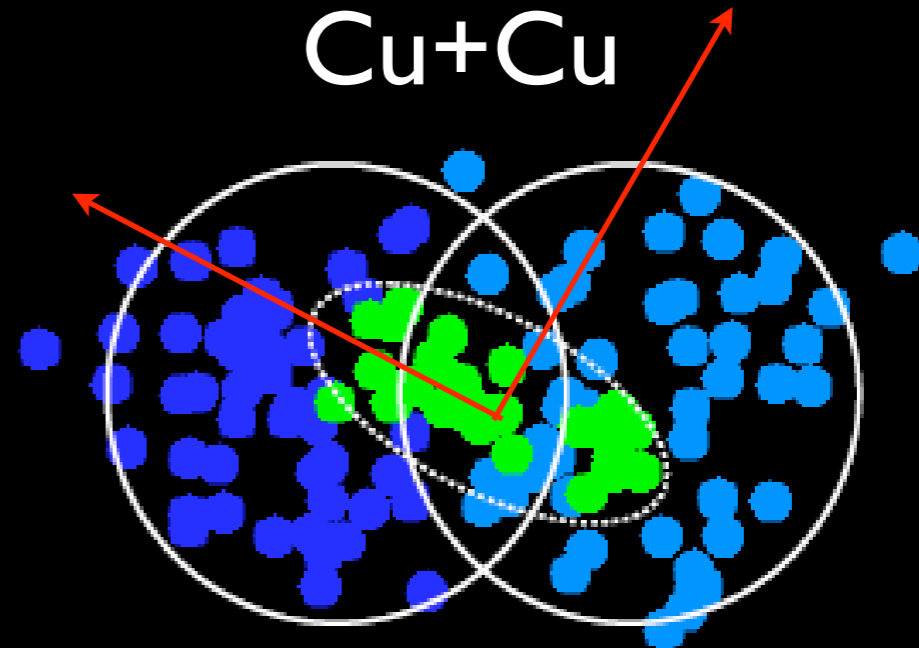
In **Glauber MC** model, geometry is sampled by finite number of nucleons → Geometry varies from event-to-event, even at fixed  $b$

Aguiar, Hama, Kodama, Osada, hep-ph/0106266 (QM 2001)  
Miller, Snellings, nucl-ex/0312008

Cu+Cu



Cu+Cu



Plots from Richard Bindel, Maryland,  
using PHOBOS Glauber MC

$$\epsilon_{part} = \frac{\sigma_y'^2 - \sigma_x'^2}{\sigma_y'^2 + \sigma_x'^2} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4(\sigma_{xy}^2)^2}}{\sigma_y^2 + \sigma_x^2}$$

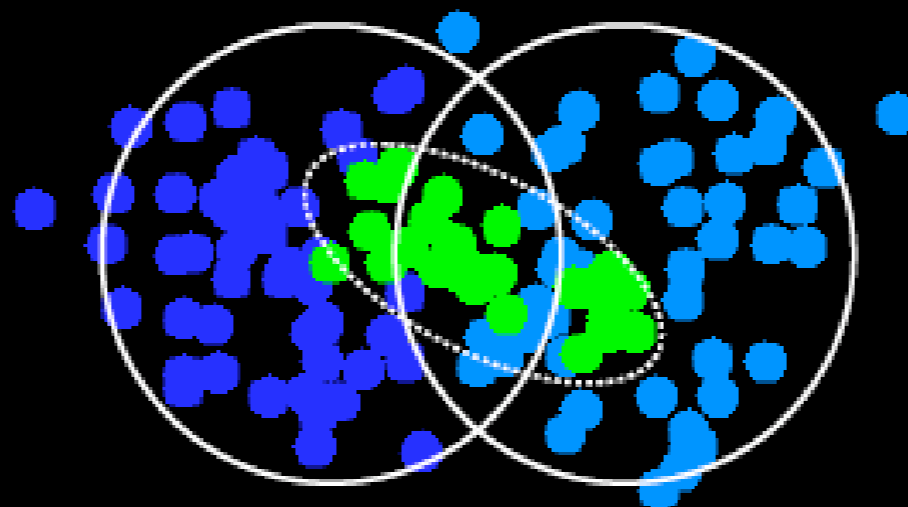
“Participant Eccentricity”

PHOBOS 2005, see also

Broniowski et al, arXiv:0706.4266

If flow is driven by initial matter distribution,  
the orientation (and shape) of that distribution  
should determine direction and magnitude of flow

Cu+Cu



How do we know the Glauber shapes and shape fluctuations are real?

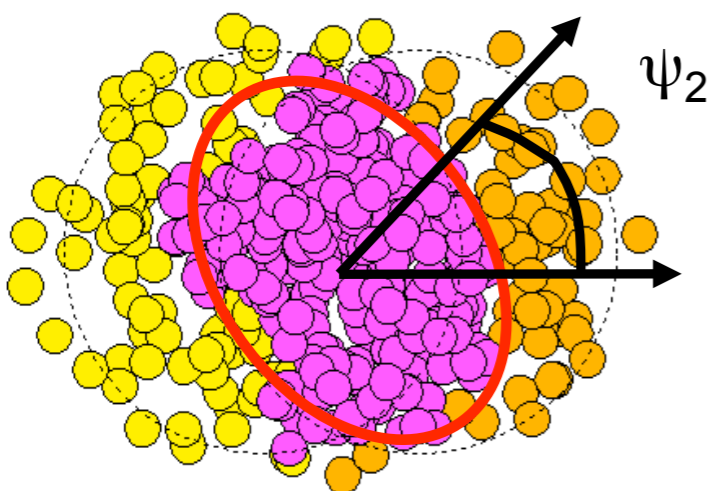
Measure them directly!

If  $v_2 \propto \epsilon$ , then:

$$\frac{\sigma(v_2)}{\langle v_2 \rangle} = \frac{\sigma(\epsilon)}{\langle \epsilon \rangle}$$

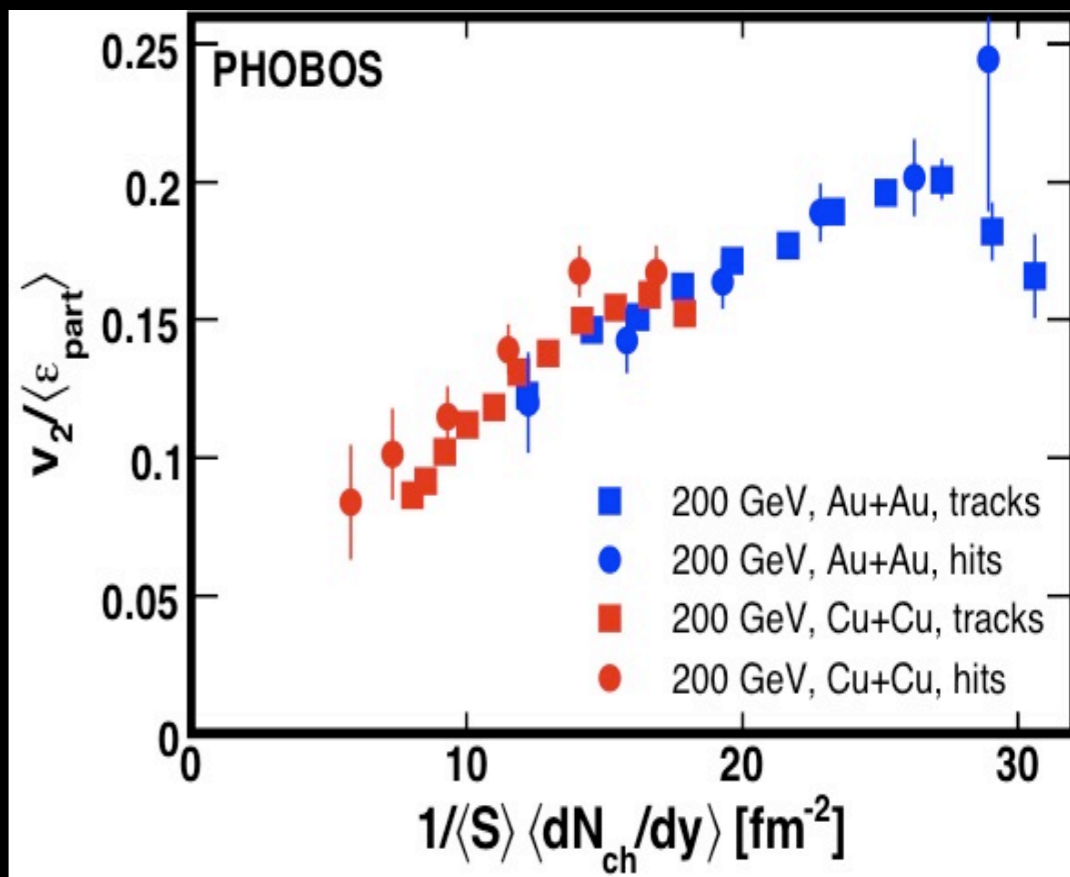
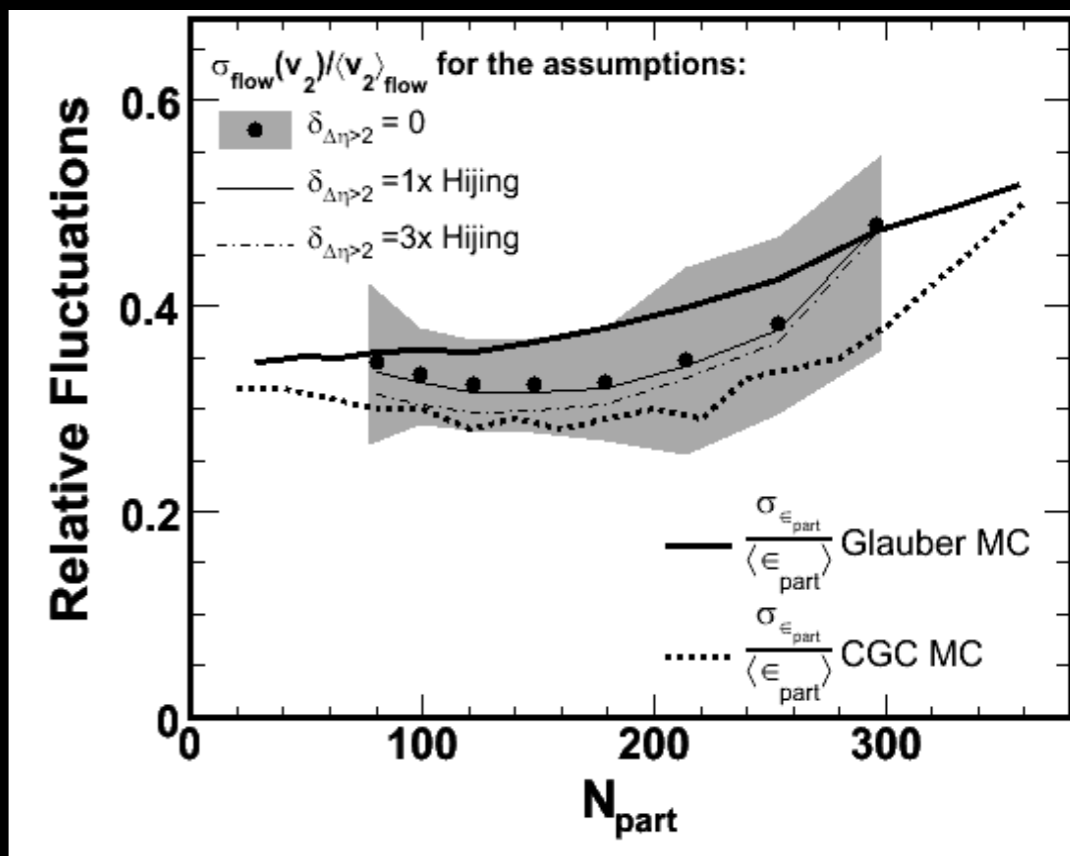
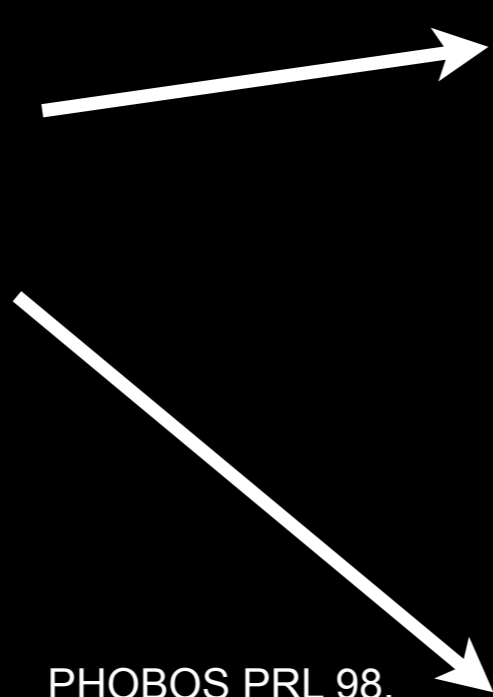
i.e. relative fluctuations in  $v_2$  should be determined by relative fluctuations in  $\epsilon$

## Participant Eccentricity

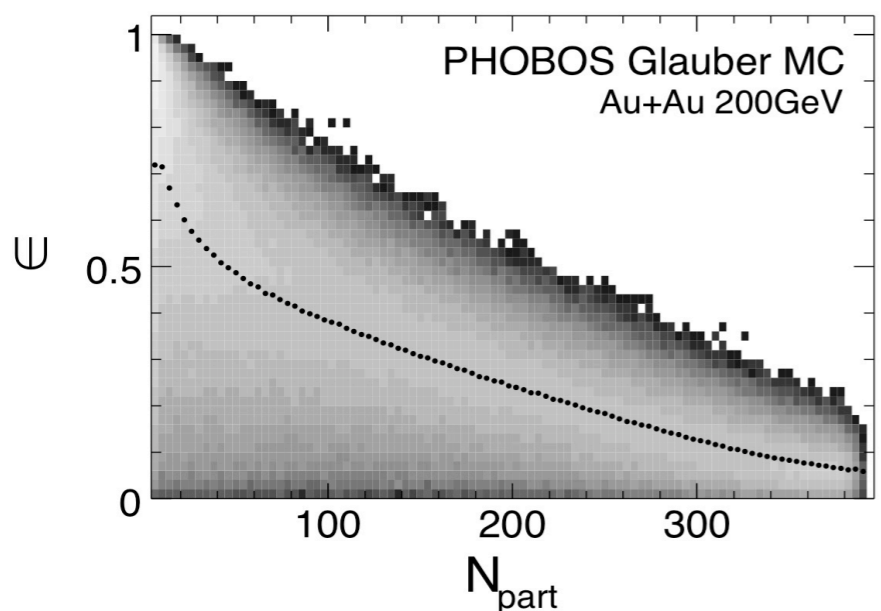


$$\epsilon = \frac{\sqrt{\langle (r^2 \cos(2\phi))^2 \rangle + \langle (r^2 \sin(2\phi))^2 \rangle}}{\langle r^2 \rangle}$$

PHOBOS PRL 104,  
142301 (2010)  
PHOBOS PRC81,  
034915 (2010)

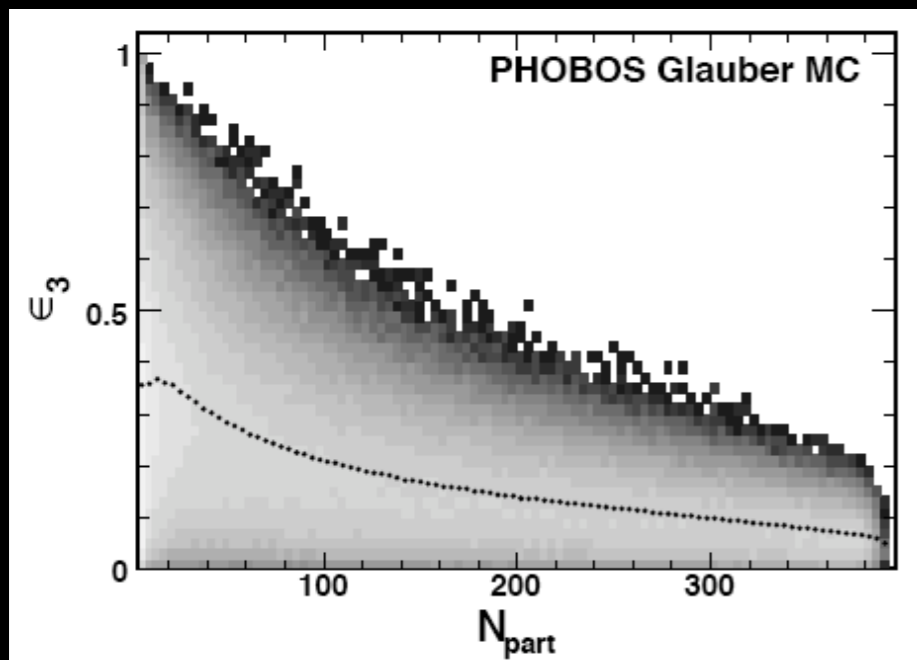
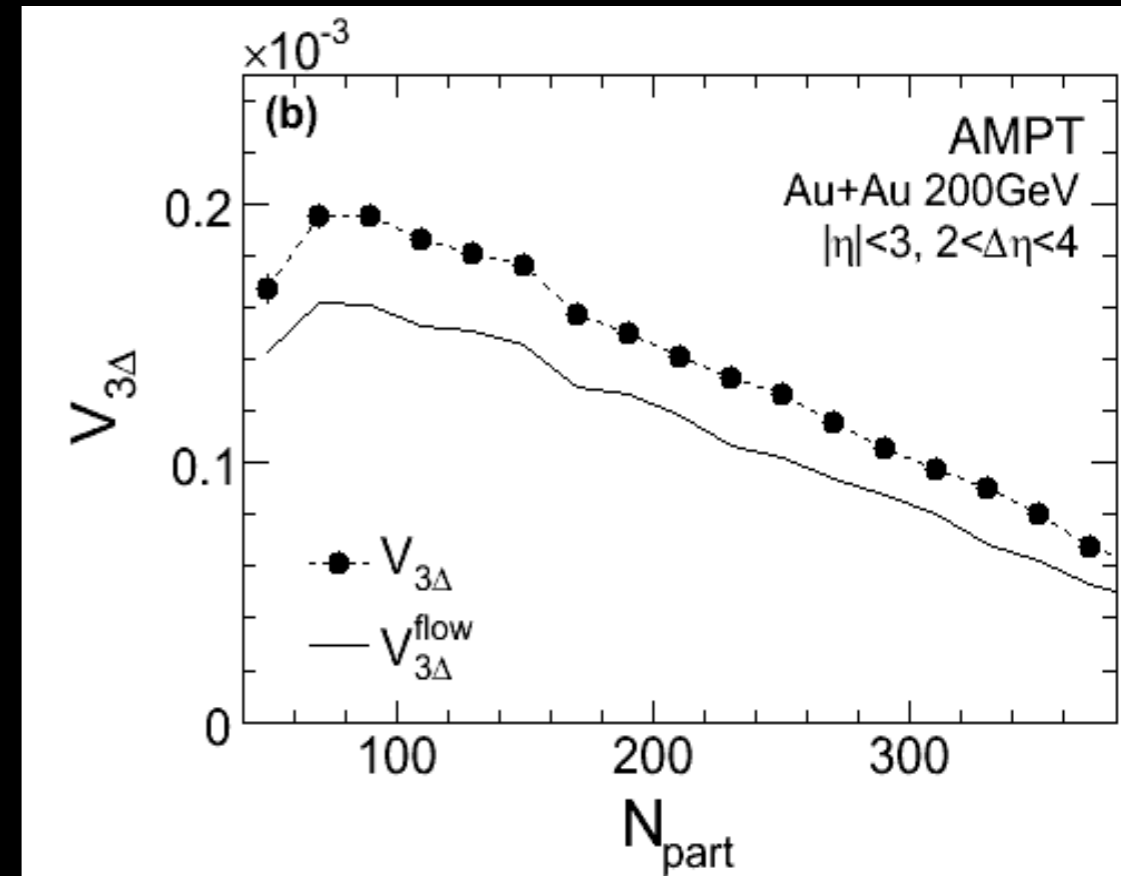
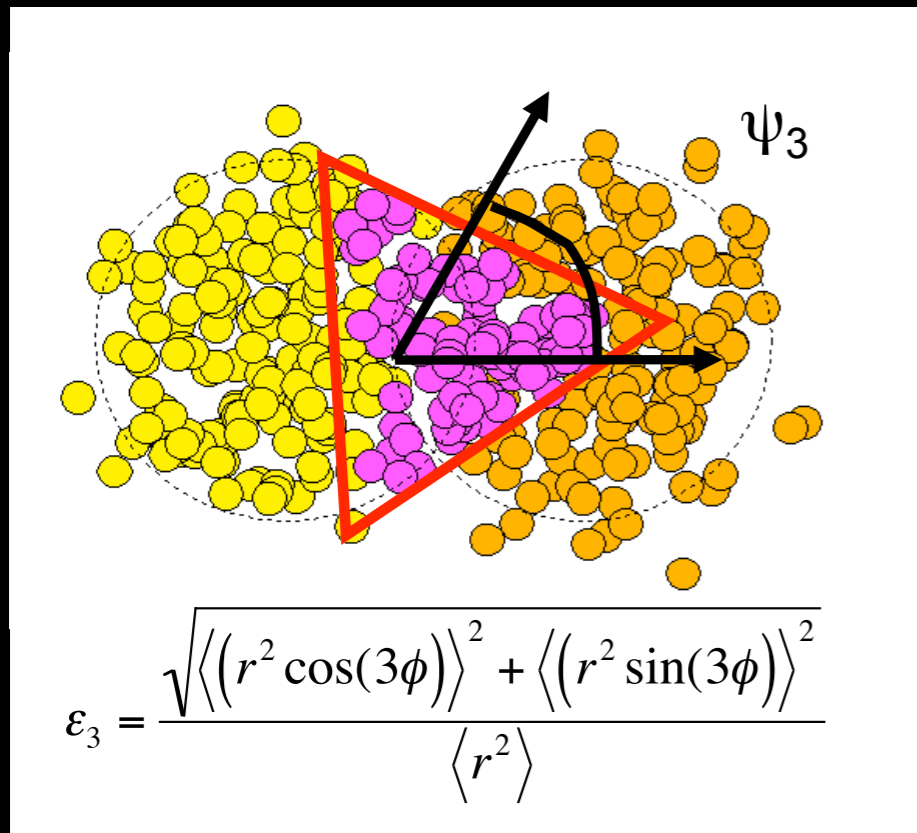


PHOBOS PRL 98,  
242302 (2007)





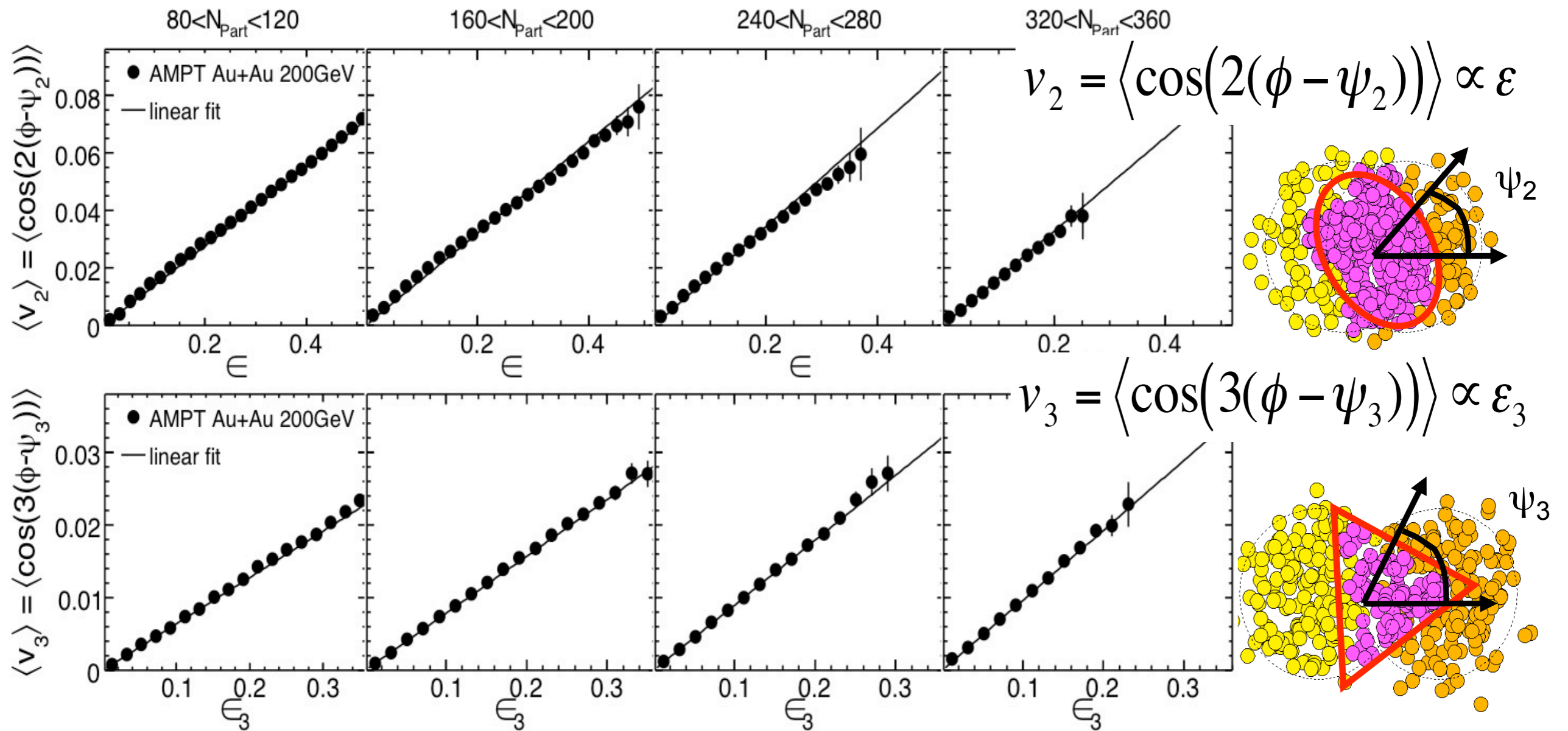
## Participant Triangularity



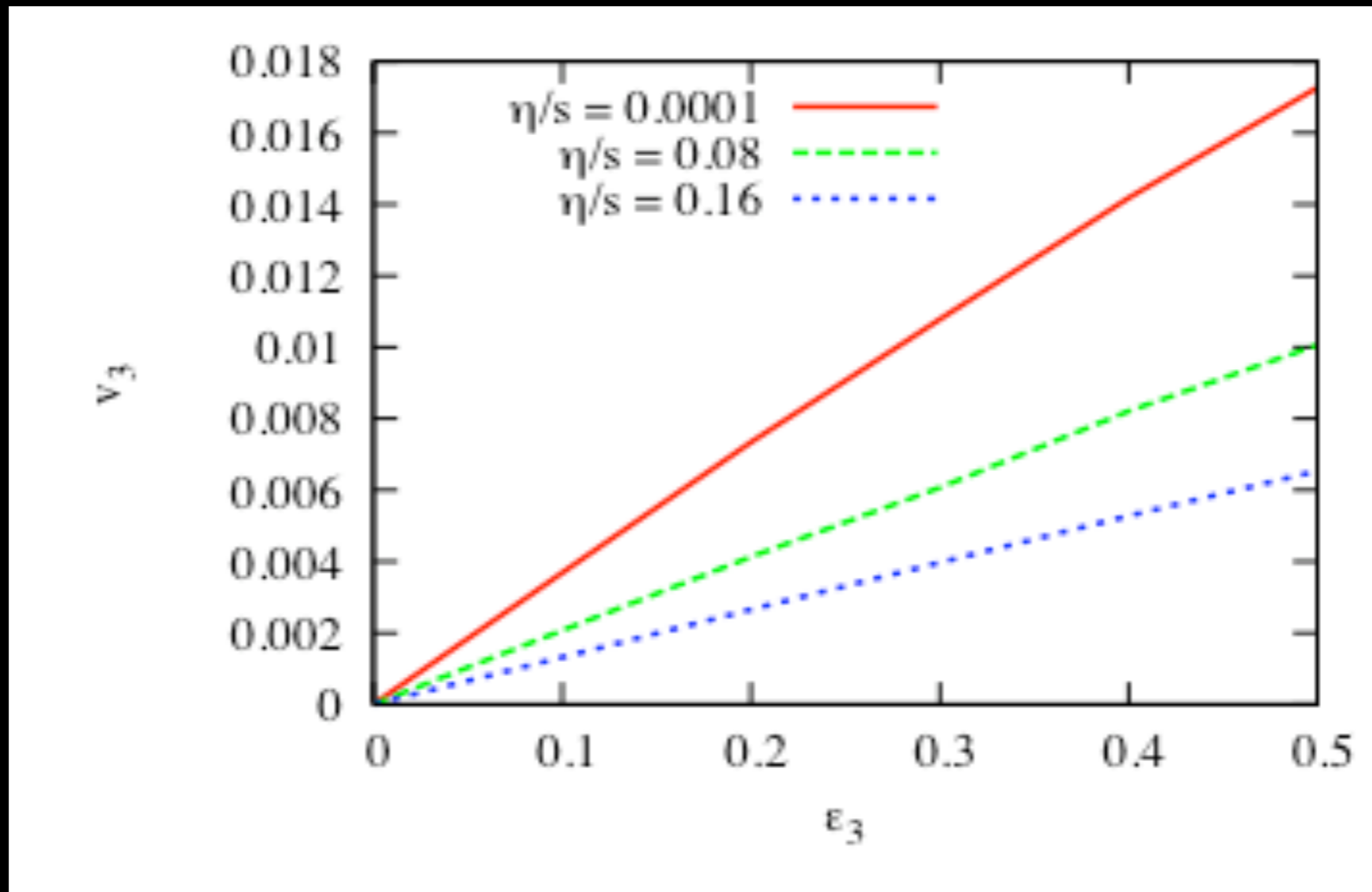
Just like elliptic flow reflects event-by-event eccentricity, “triangular flow” ( $v_3$ ) reflects event-by-event “triangularity” ( $\varepsilon_3$ )



# Elliptic and triangular flow

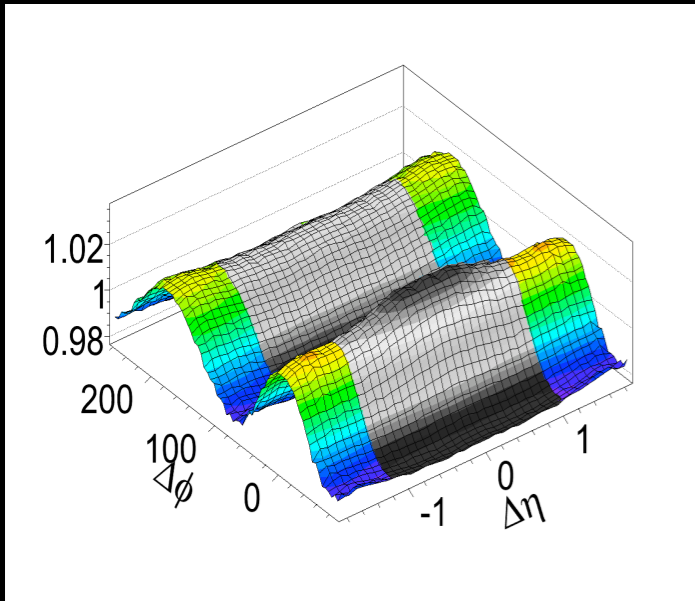


Burak Alver, GR, arXiv:1003.0194 (PRC in press)

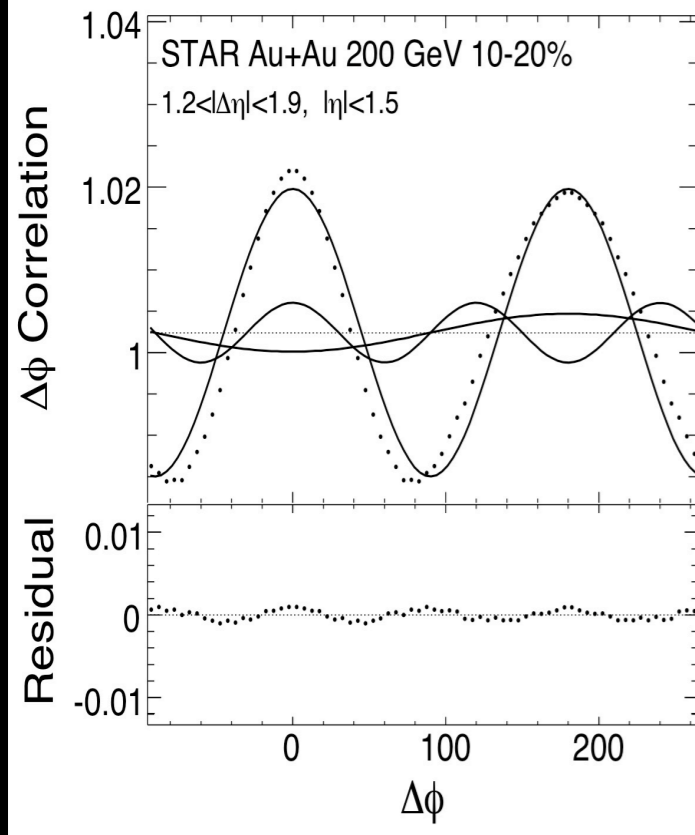


Triangular flow in hydro calculations, not just AMPT  
Luzum, Ollitrault, private communication

## Inclusive correlations

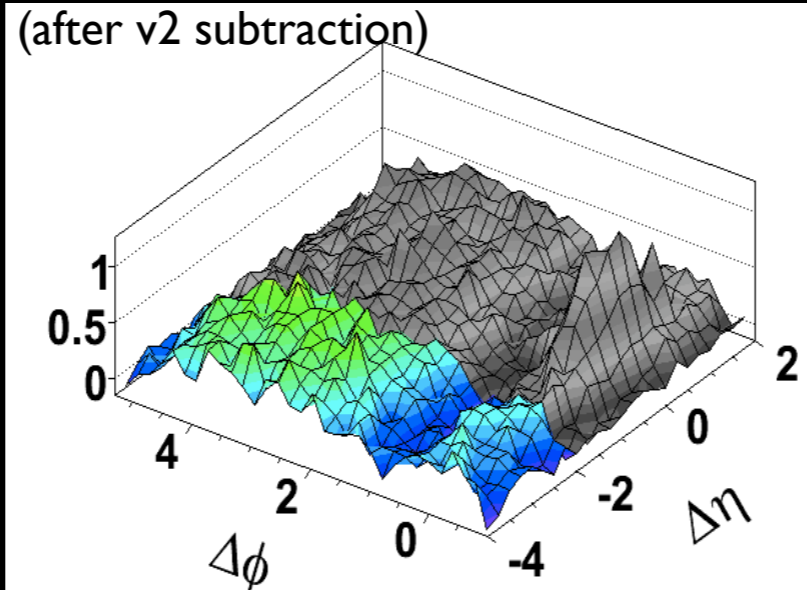


arXiv:0806.0513

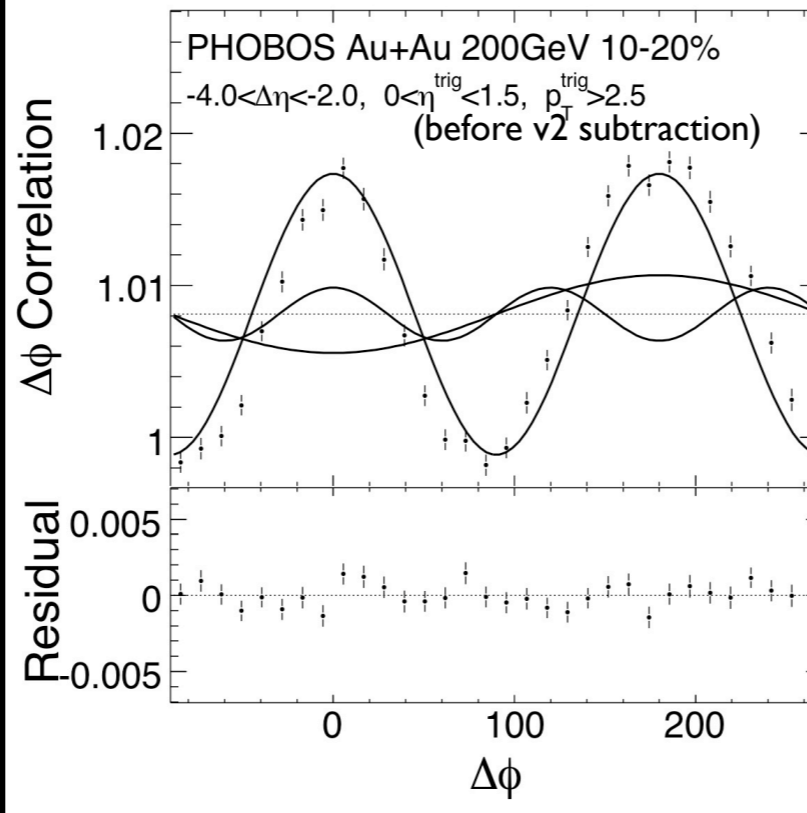


## Triggered correlations

(after  $v_2$  subtraction)



PRL 104, 06230 (2010)



Published correlation data (STAR, PHOBOS) show  $v_3$  component!

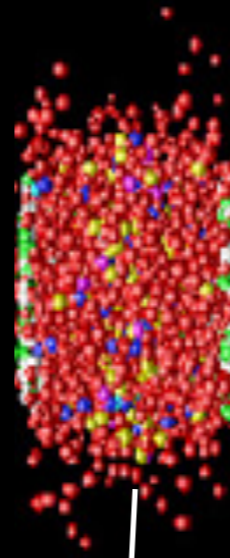
Flow contribution to long-range “ridge” and “broad away-side”

This is purely a fluctuation effect - no fluctuations, no  $v_3$ !

n.b.  $\Psi_2$  and  $\Psi_3$  are uncorrelated - triangular flow is not visible in  $v_2$  event plane analysis

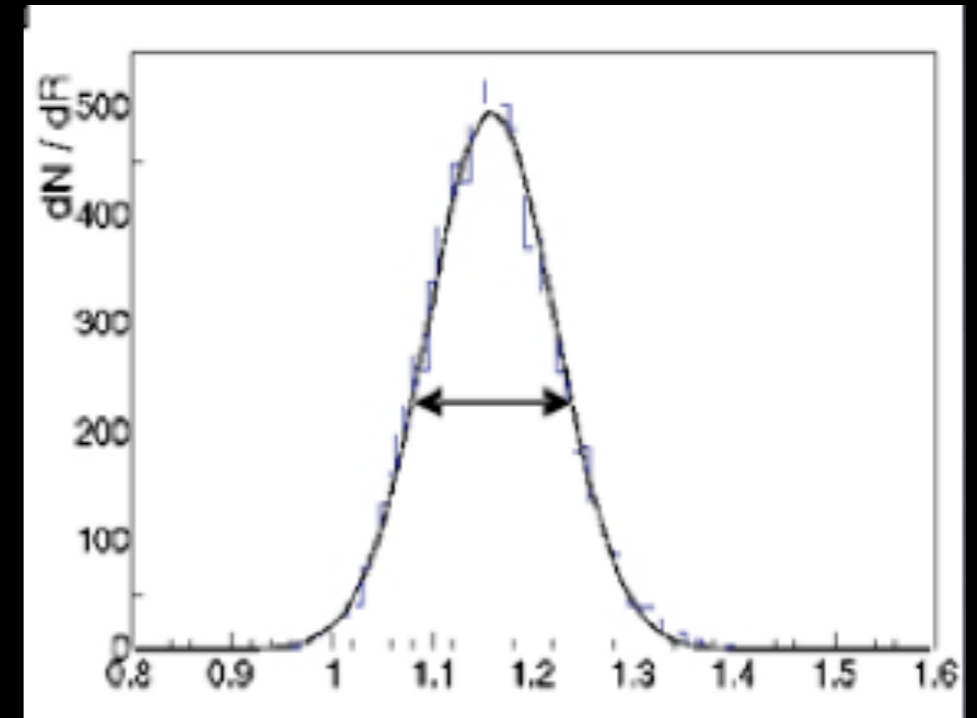


QGP



Hydrodynamic expansion

Fluctuations of conserved quantum numbers

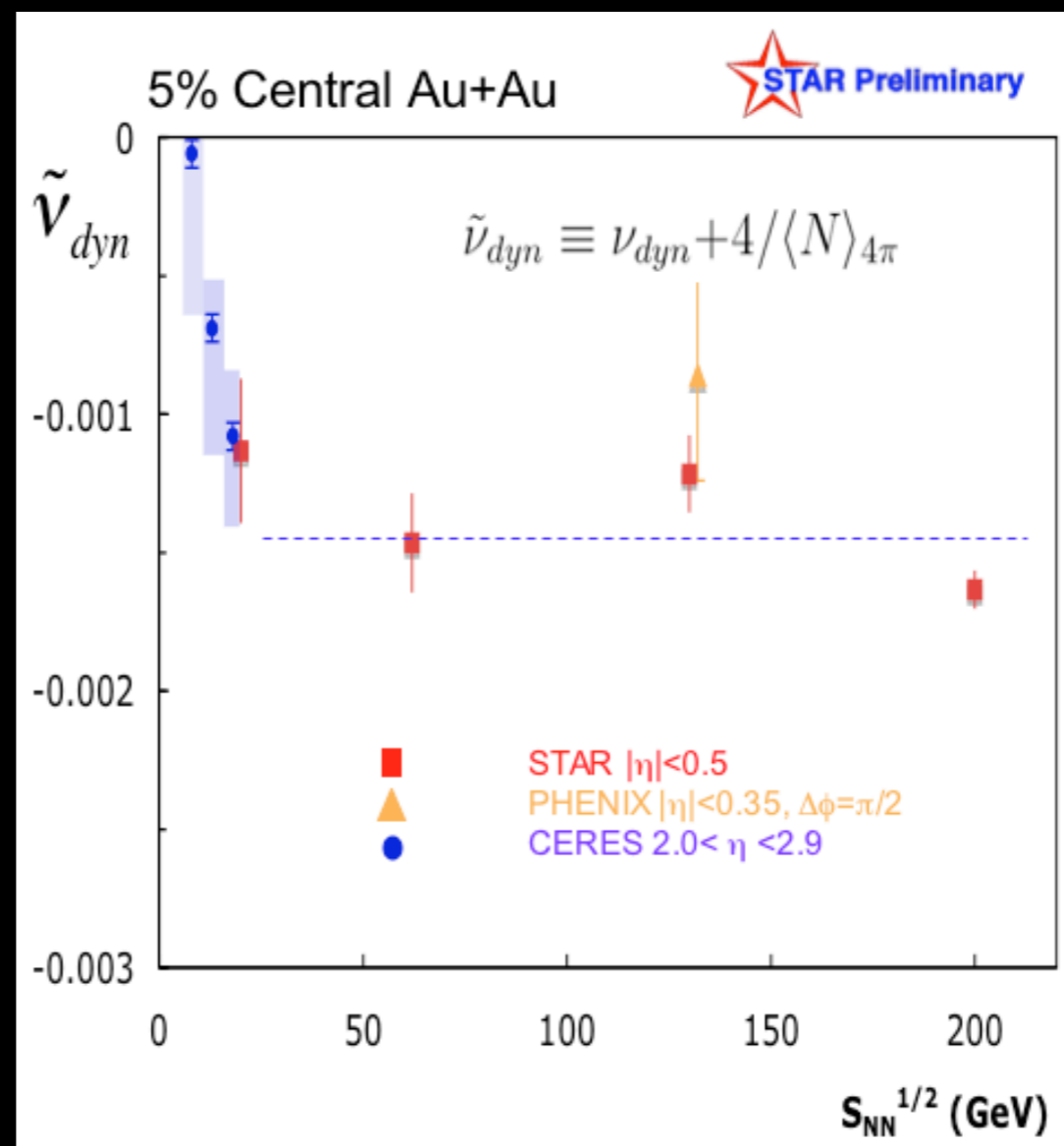
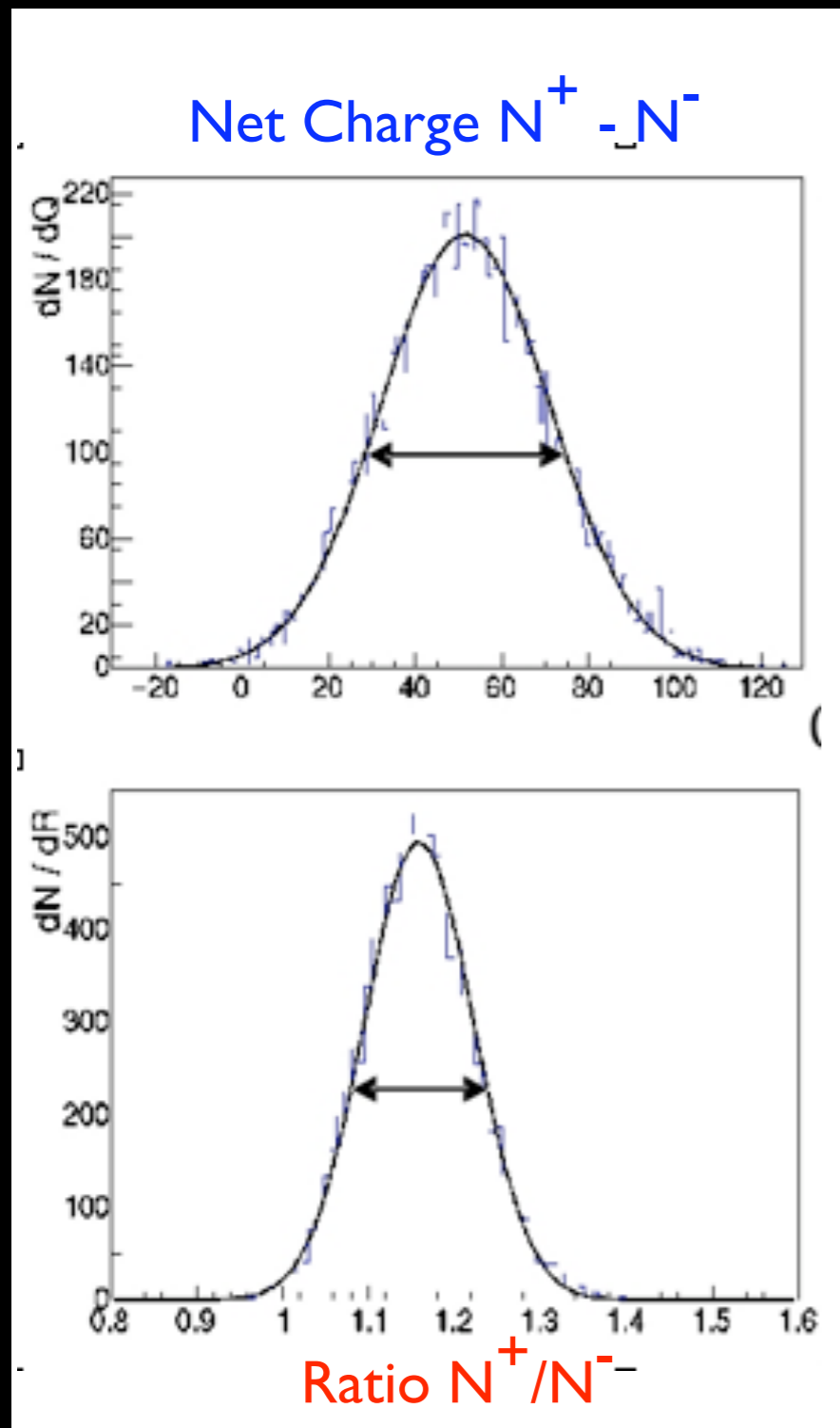


Event-by-event distribution of net charge ratio

- **Net Charge/ $\Delta y$  Fluctuations  $\Leftrightarrow$  Charge/DoF**
  - Fluc's change from **1-2 (QGP)** to **4 (Pion Gas)**
- **Fluctuations frozen b/c charge conservation**
  - Diffusion vs Expansion timescale

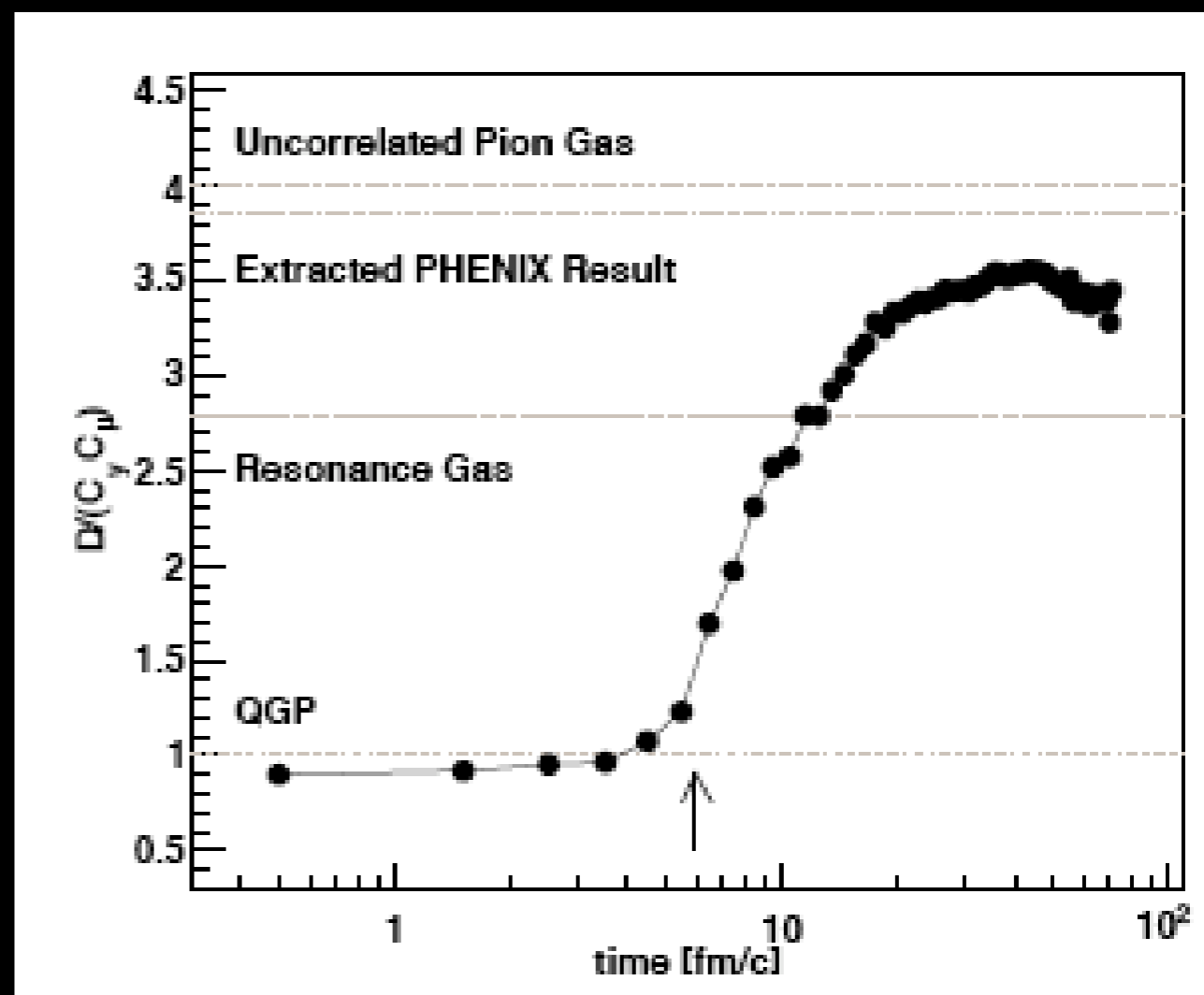
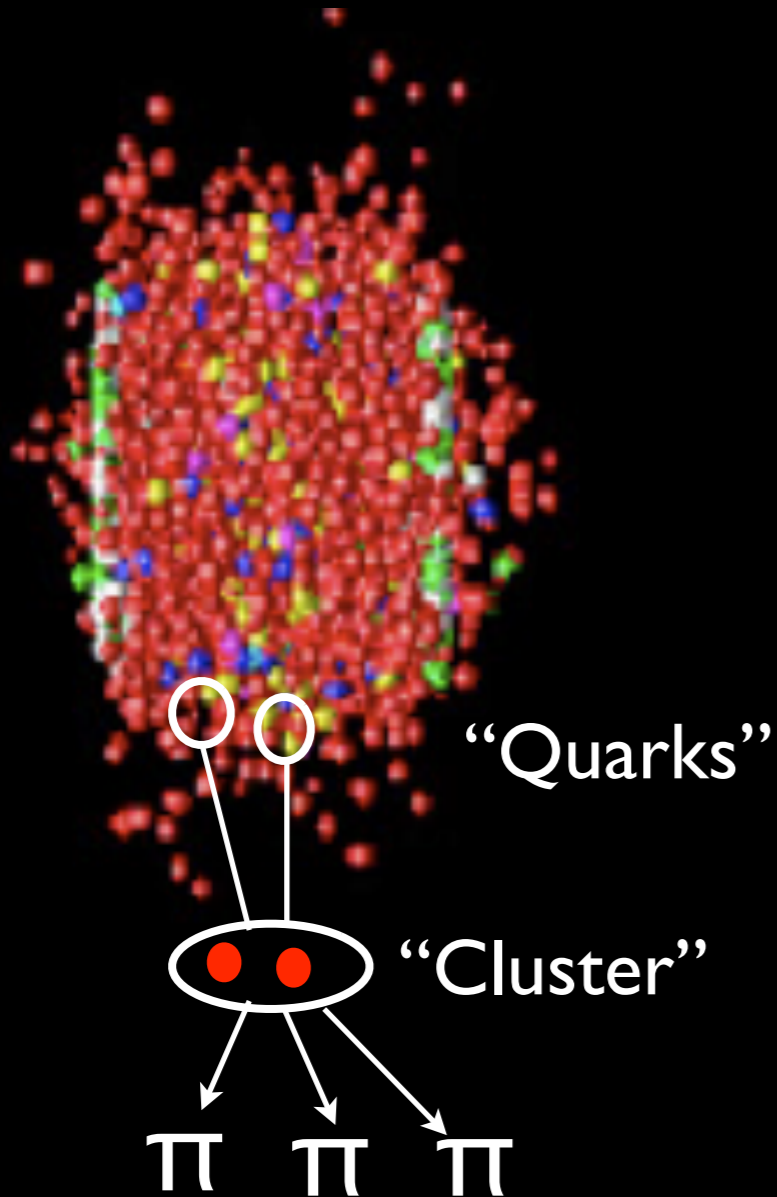
Plot from Claude Pruneau  
RHIC Users meeting workshop '04

PHENIX: PRL 89 082301 (2002)



QGP



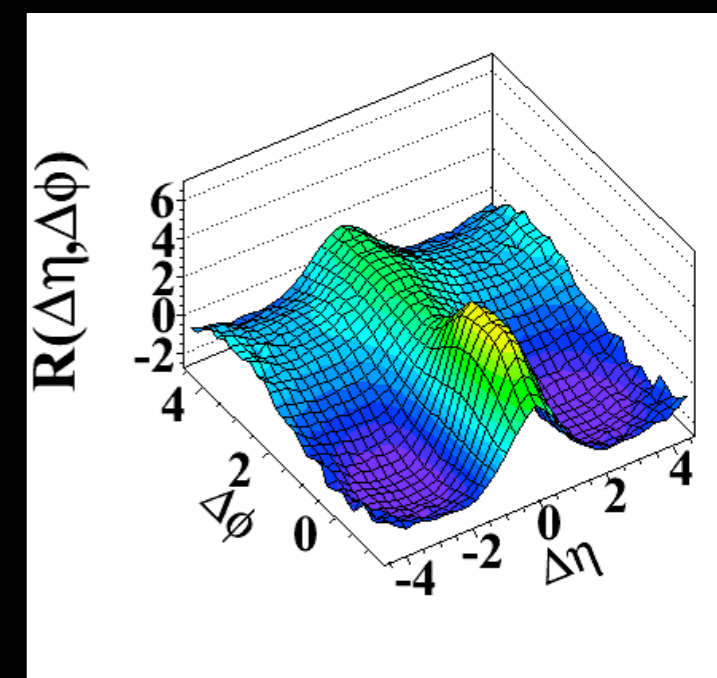
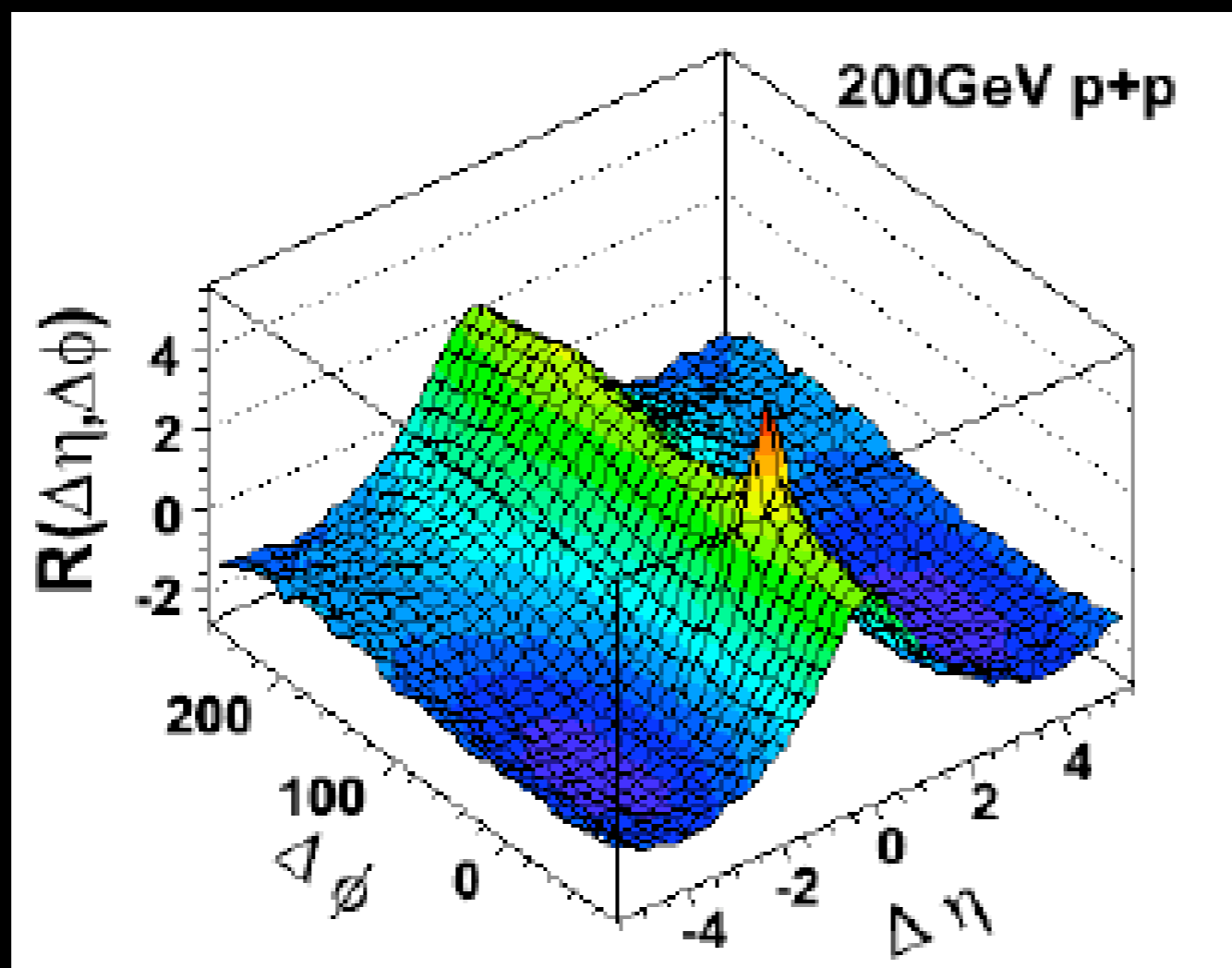


Recombination of “quarks” into “clusters” and subsequent decay of clusters provides redistribution of charges

$$R(\Delta\eta) = \langle (n-1) \left( \frac{\rho(\eta_1 - \eta_2)}{\rho_{mix}} - 1 \right) \rangle$$

PHOBOS (2008)

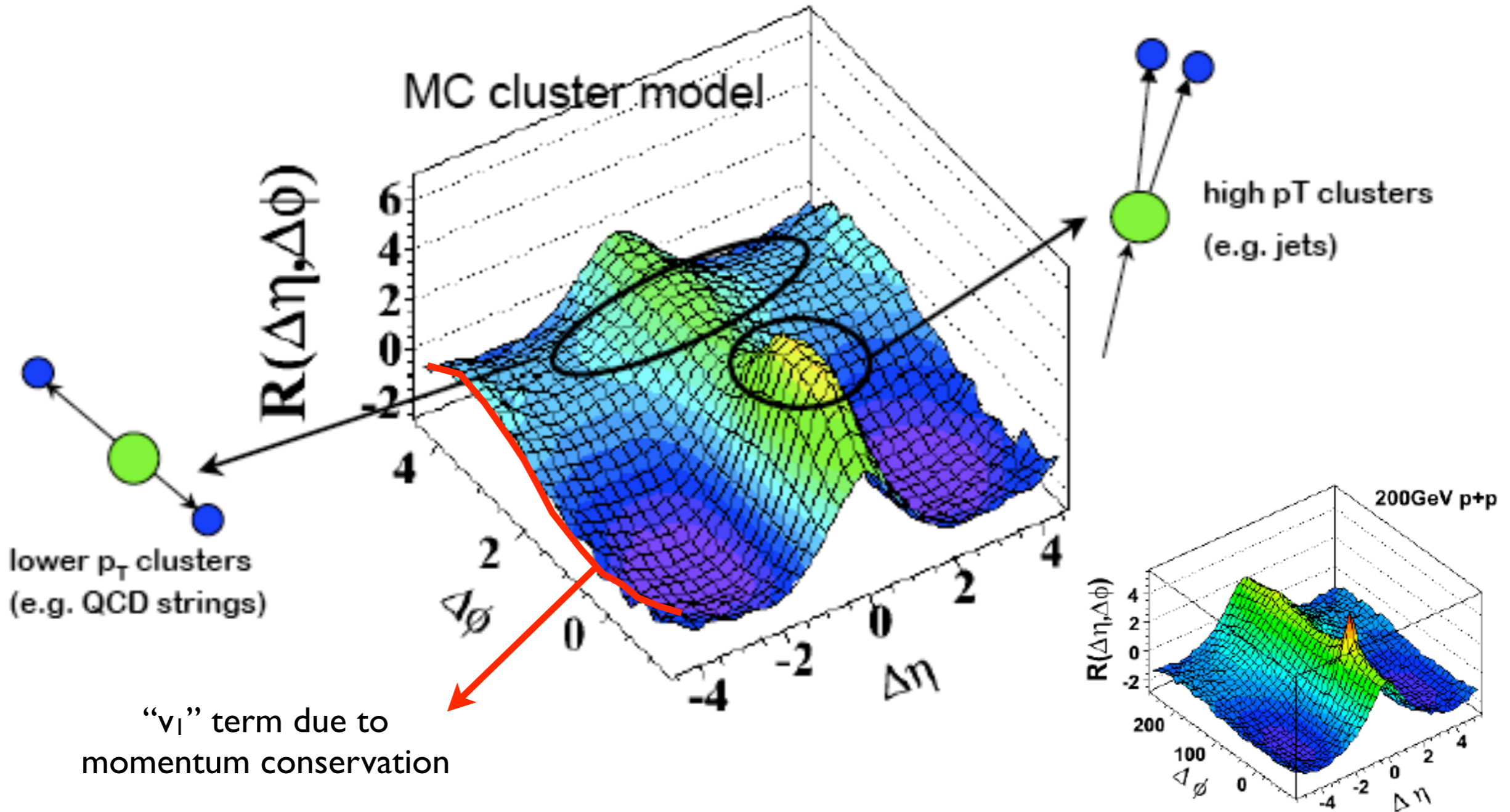
Cluster MC



Particles are not produced independently

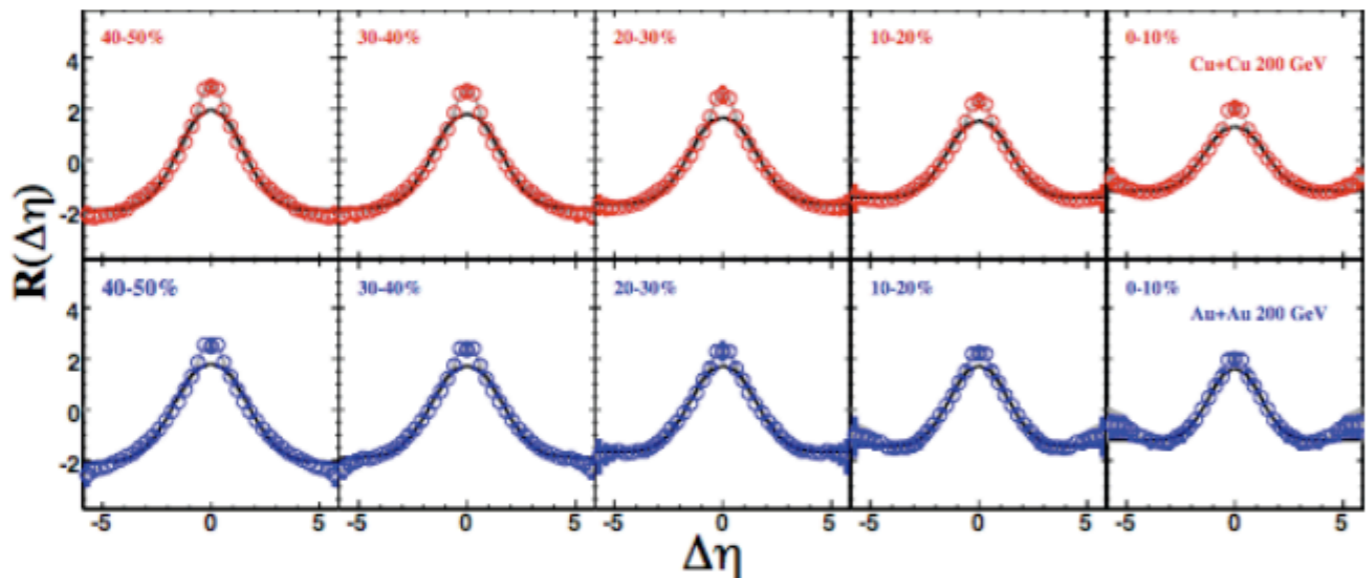
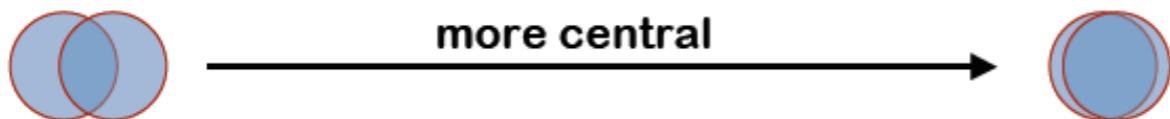


MC cluster model

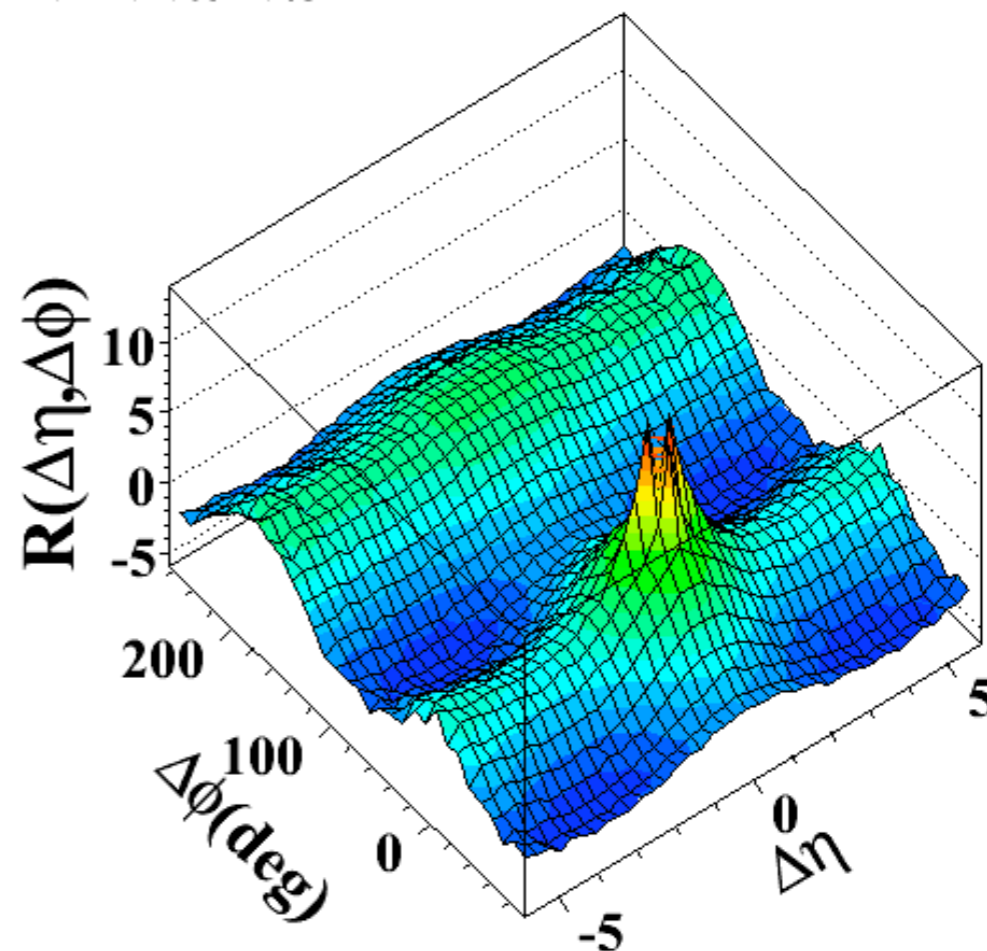


PHOBOS (2010)

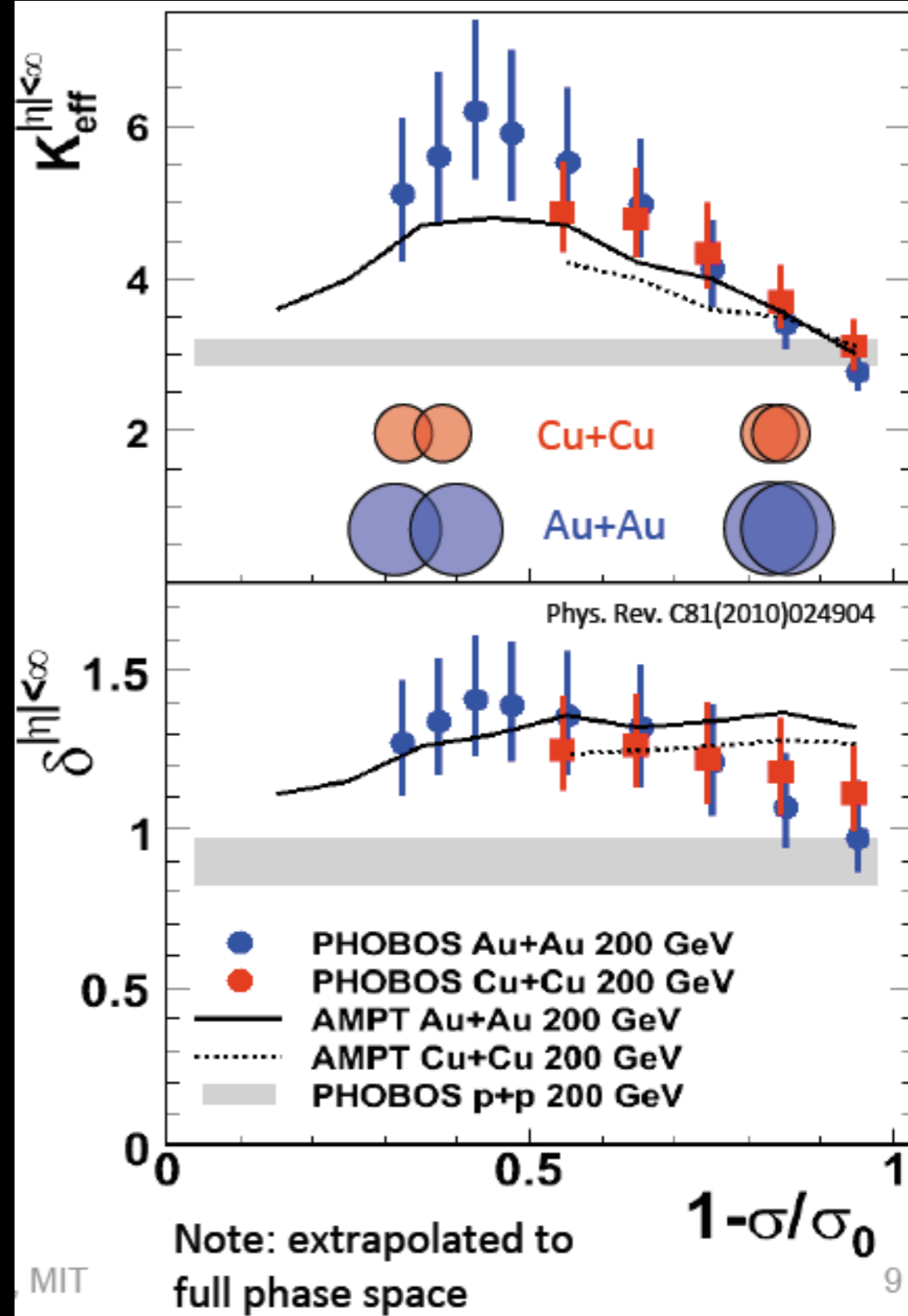
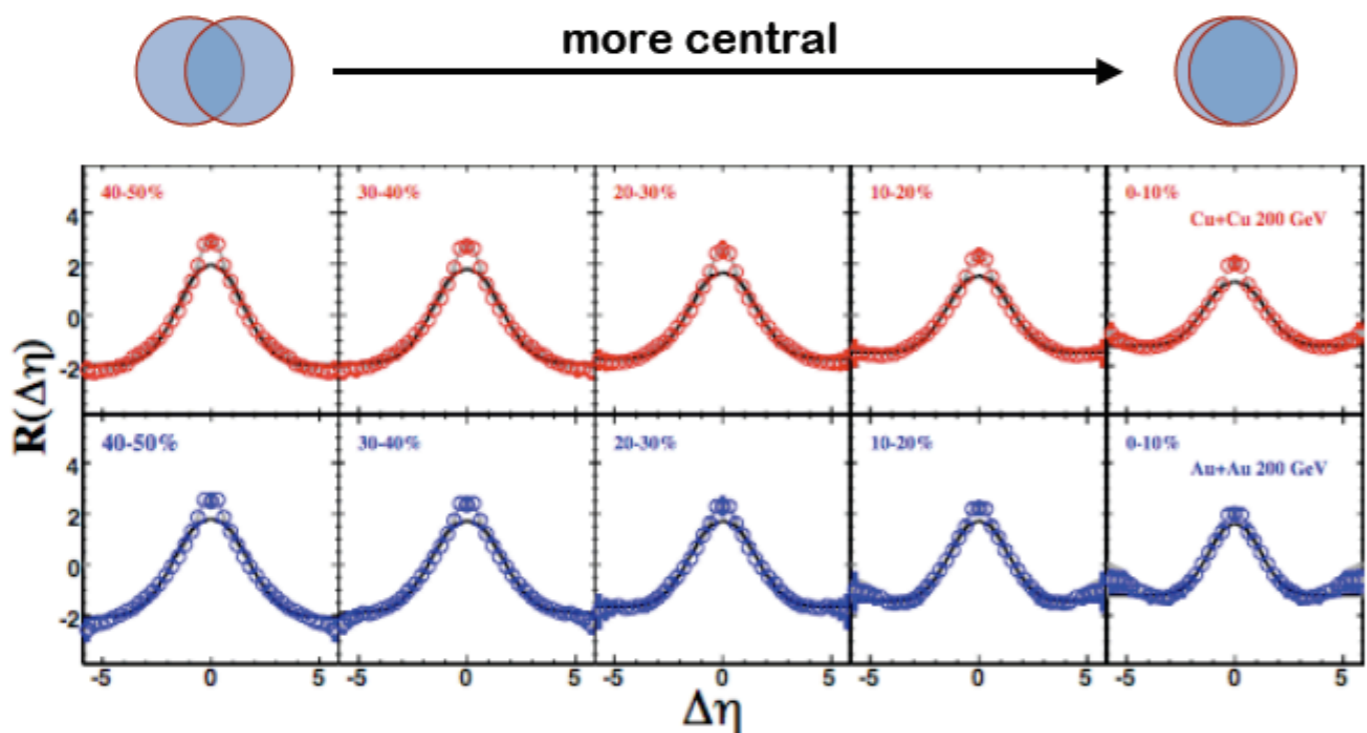
## Two-particle $\Delta\eta$ correlation function



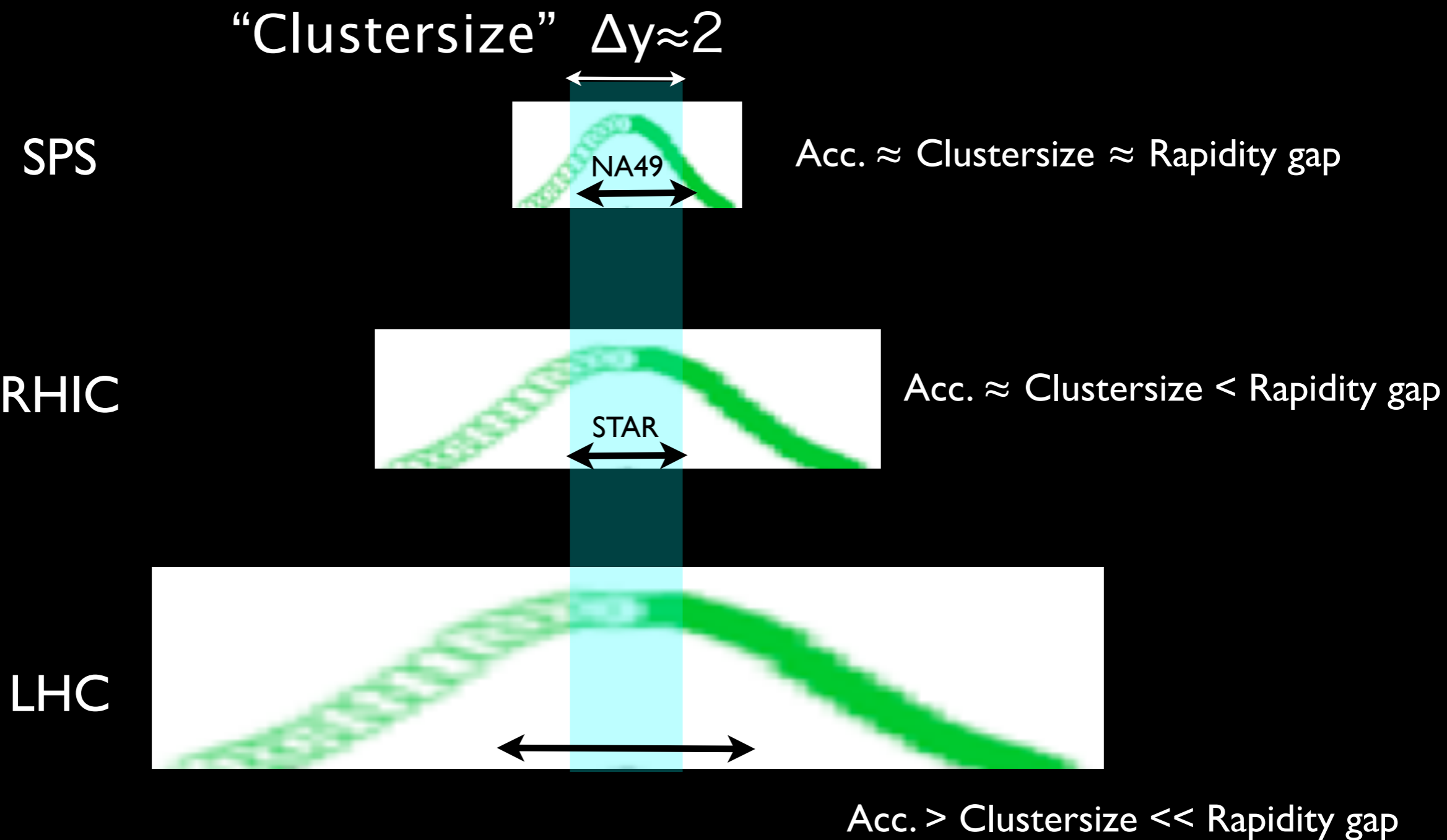
Au+Au 0%-10%



## Two-particle $\Delta\eta$ correlation function



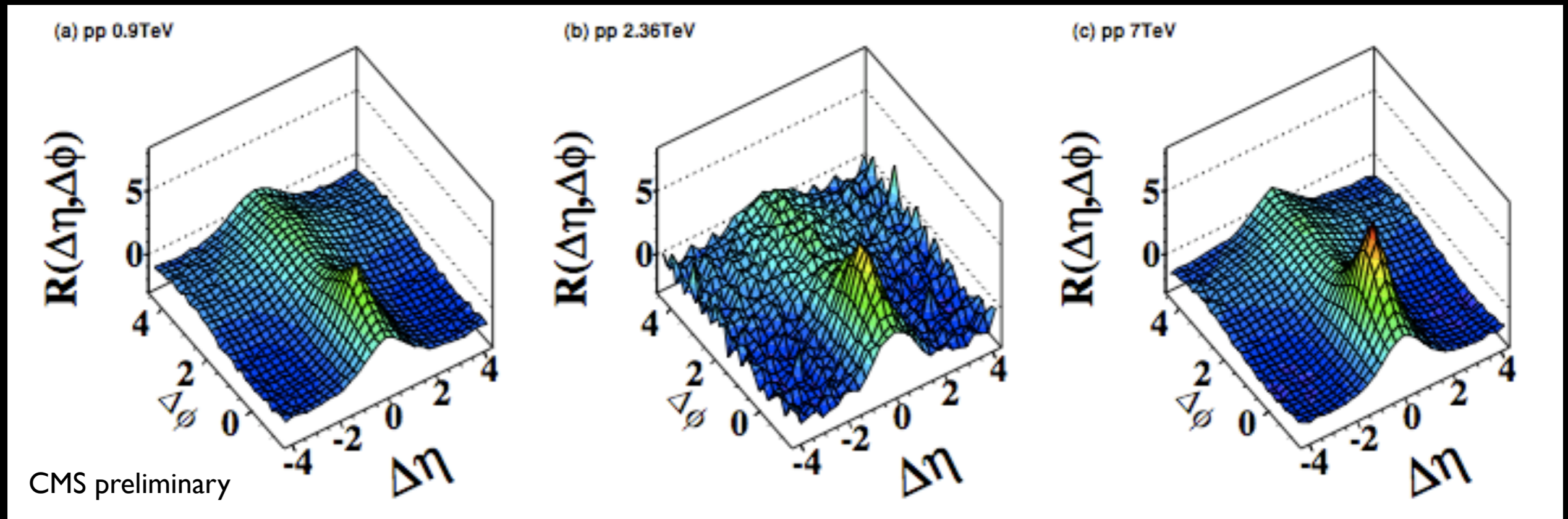
# Try again at LHC?







# Two-particle correlations at LHC

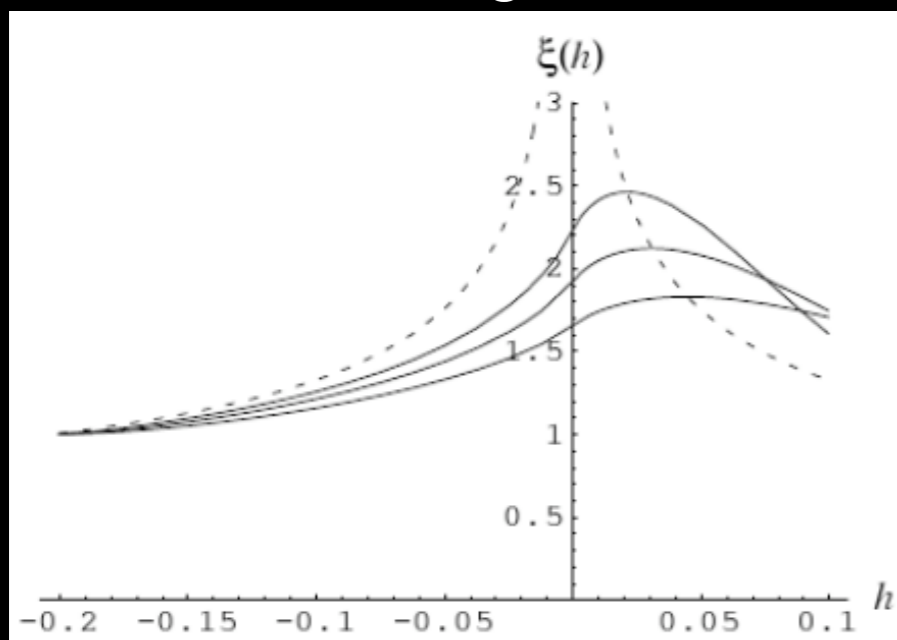


pp correlation functions from CMS

Correlation functions show increasing contribution from hard scattering

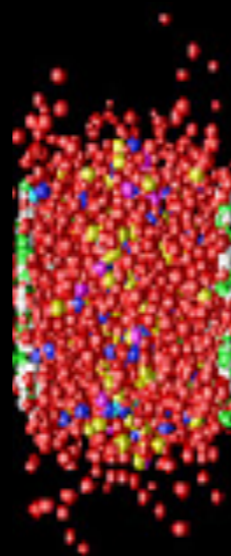


## Correlation length near CP

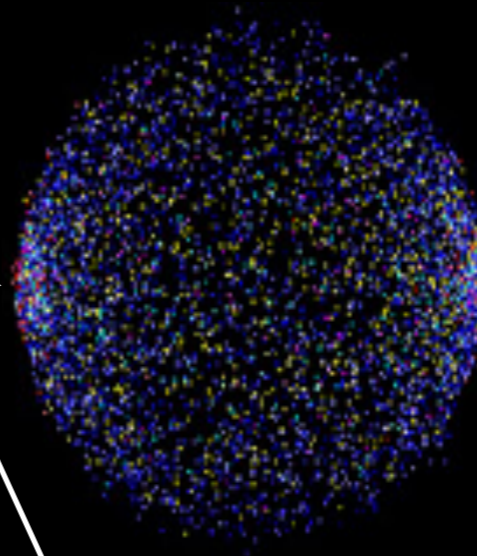


Stephanov, Rajagopal Shuryak (1998)+...

## QGP



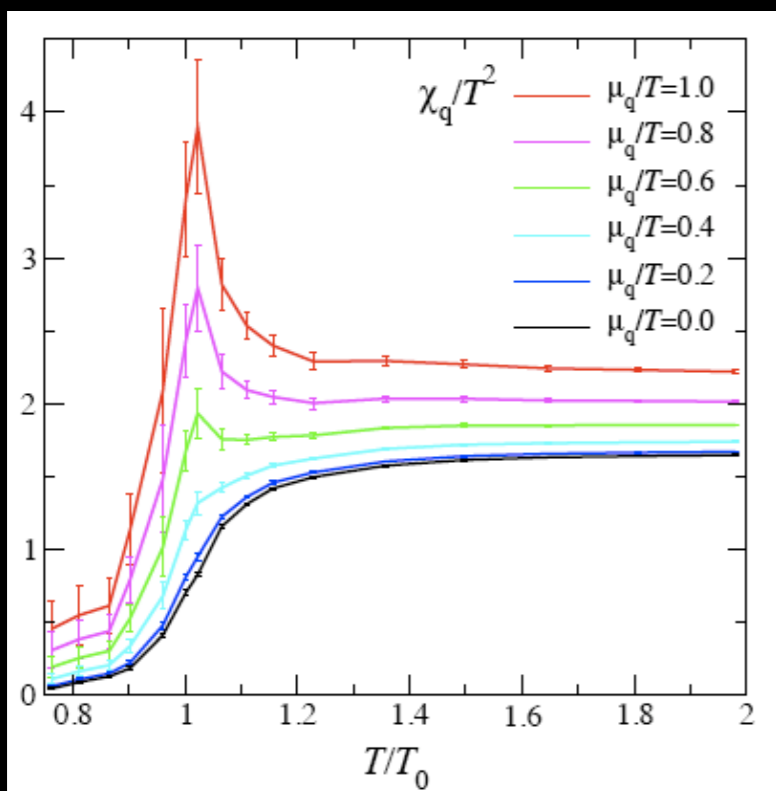
## Hadron Gas



Phase transition

Critical fluctuations;  
supercooling/bubble  
formation; cluster  
formation

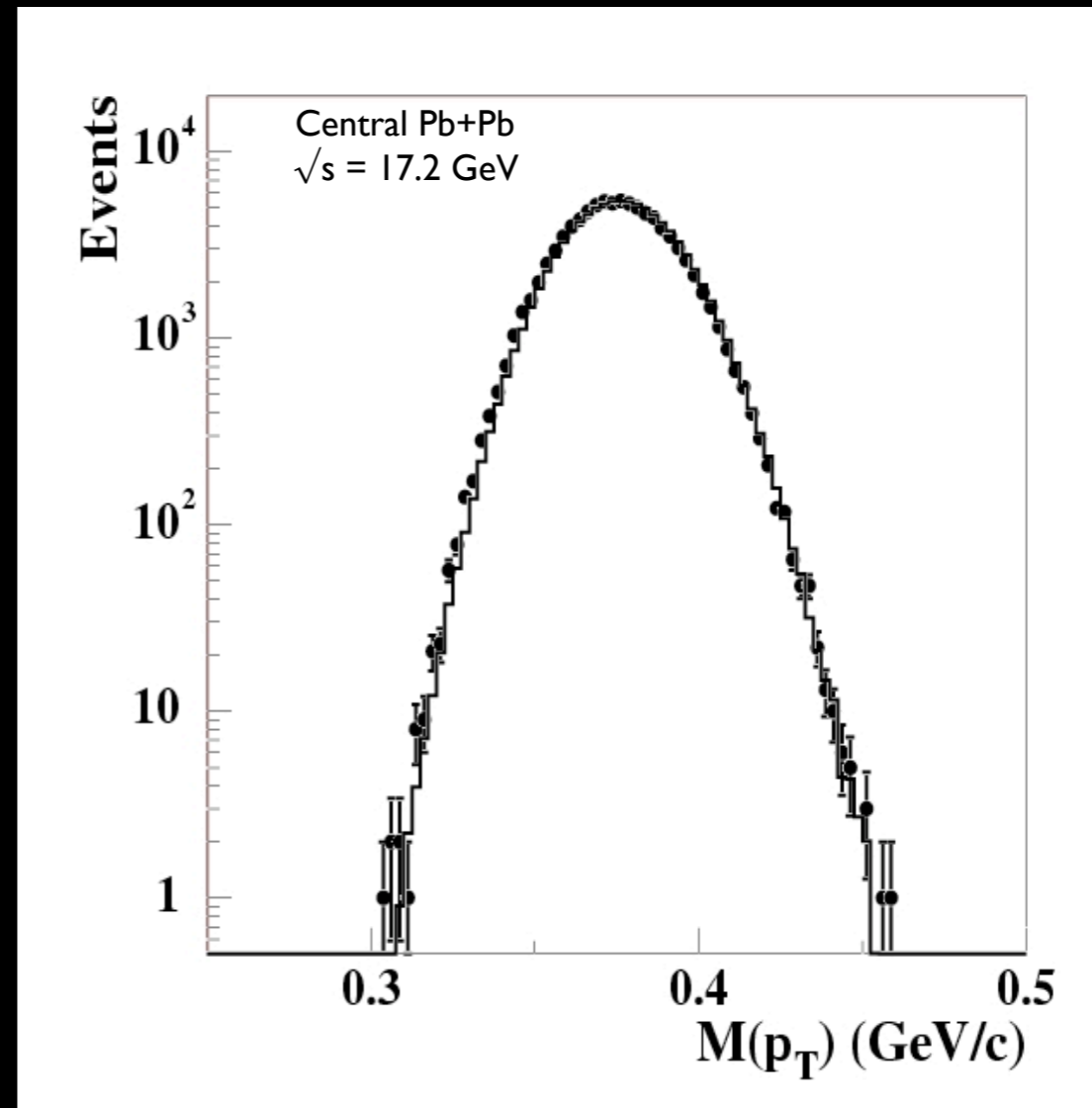
## Quark-number susceptibility near CP



Karsch et al (2003)

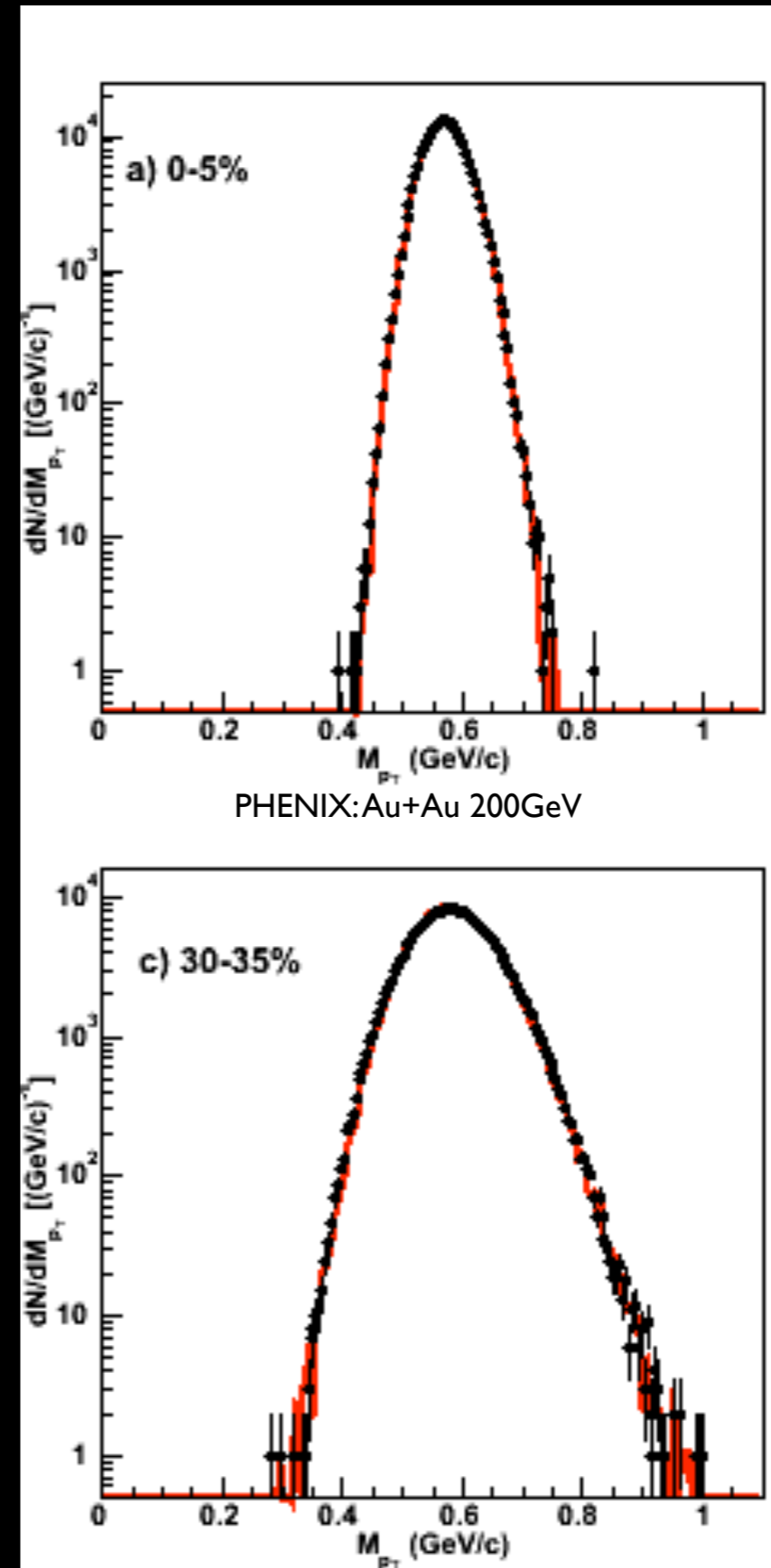
- $p_T$  - simple observable (supposedly...)
- High statistical precision:
  - $\sigma_{p_T}/\langle p_T \rangle_{inc} < 0.1\%$
- Sensitive to many interesting scenarios
  - Critical Point
  - DCC production
  - Droplet formation
  - **Any non-statistical, momentum-localized process**

NA49, Phys Lett B459 (1999) 679



Event-by-event  $\langle p_T \rangle$  compared to stochastic reference (mixed events)

- $p_T$  - simple observable (supposedly...)
- High statistical precision:
  - $\sigma_{p_T}/\langle p_T \rangle_{inc} < 0.1\%$
- Sensitive to many interesting scenarios
  - Critical Point
  - DCC production
  - Droplet formation
  - **Any non-statistical, momentum-localized process**

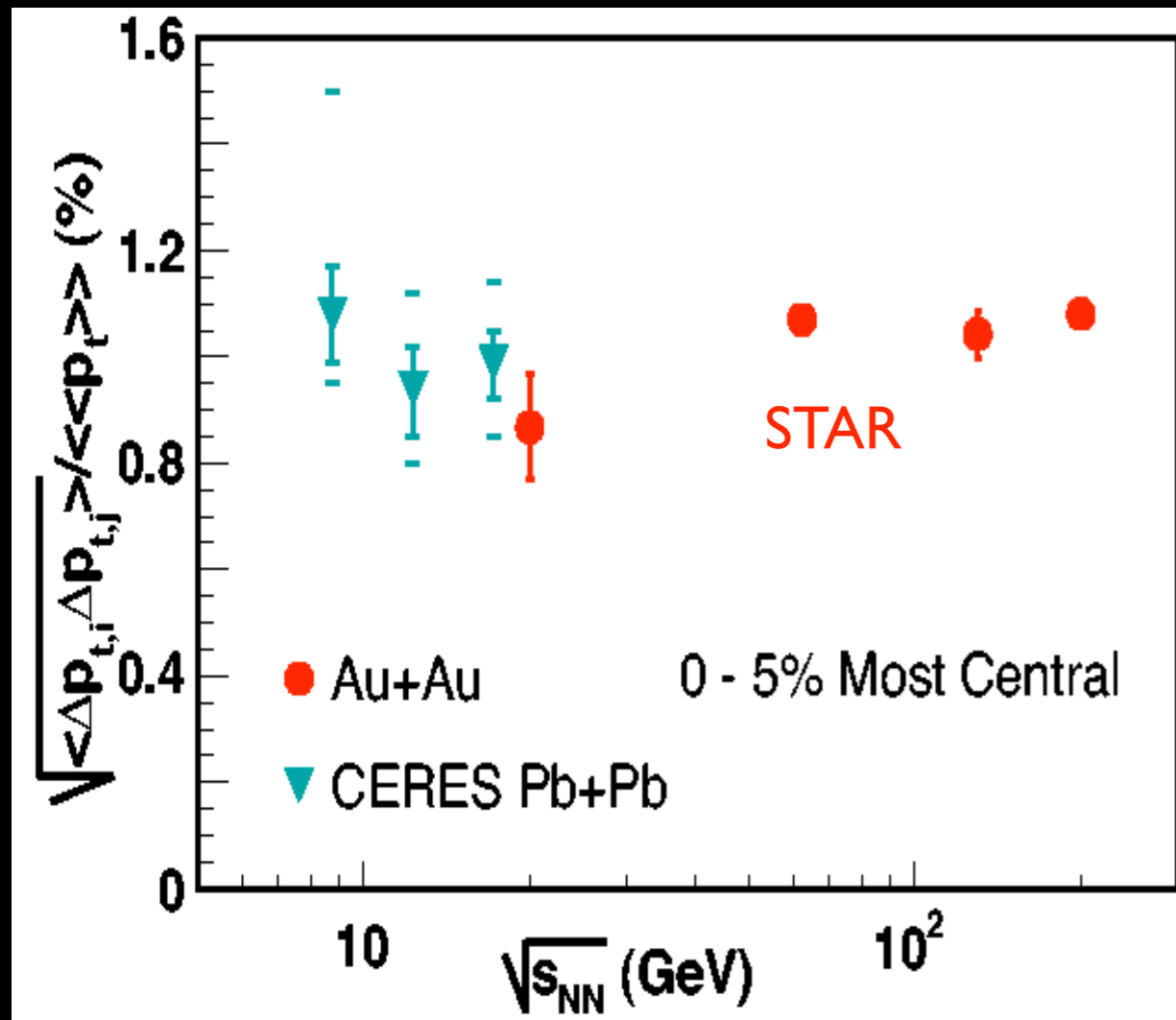




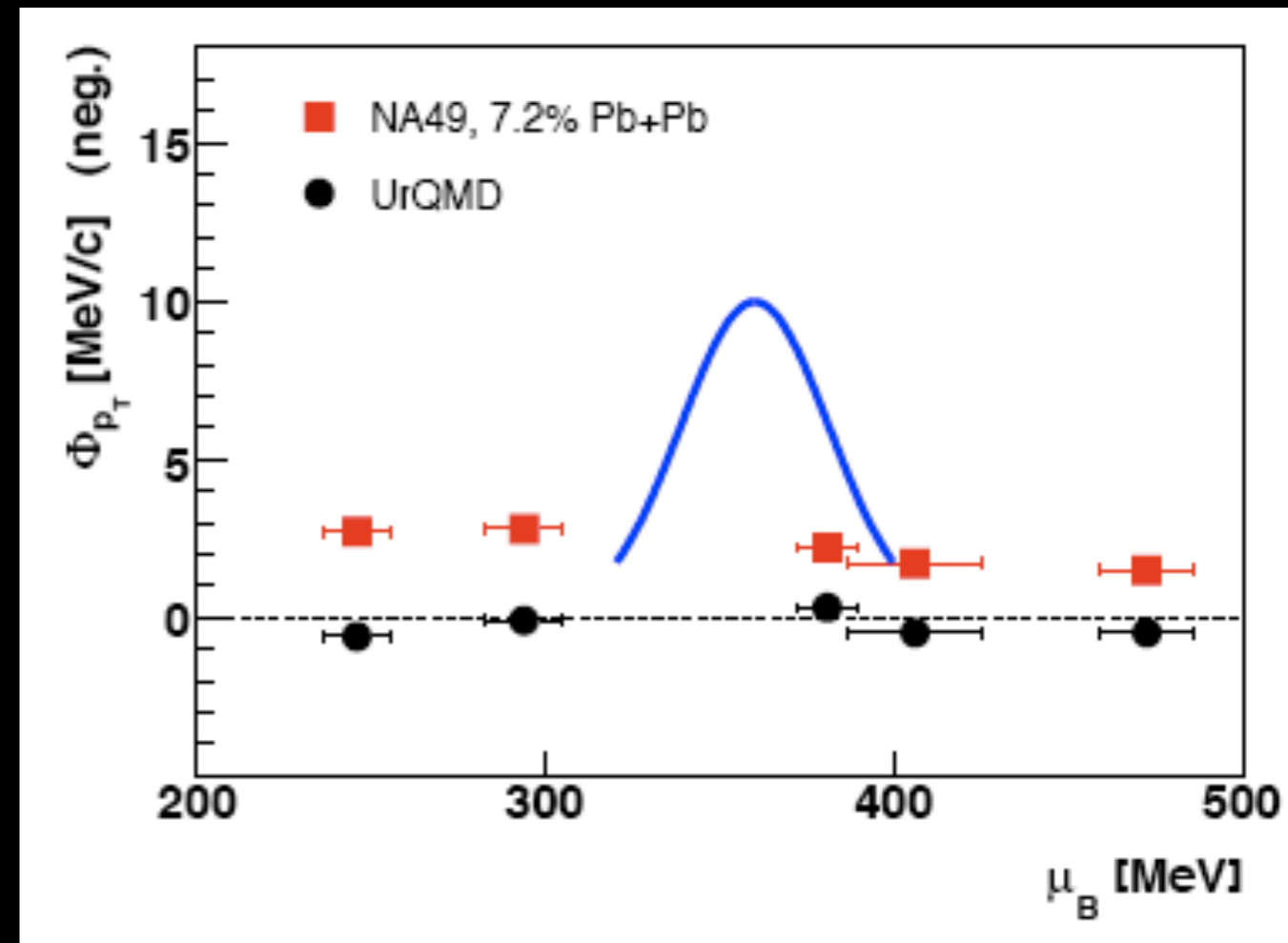
# $\langle p_T \rangle$ Fluctuations vs $\sqrt{s}$



STAR PRC 72 044902 (2005)

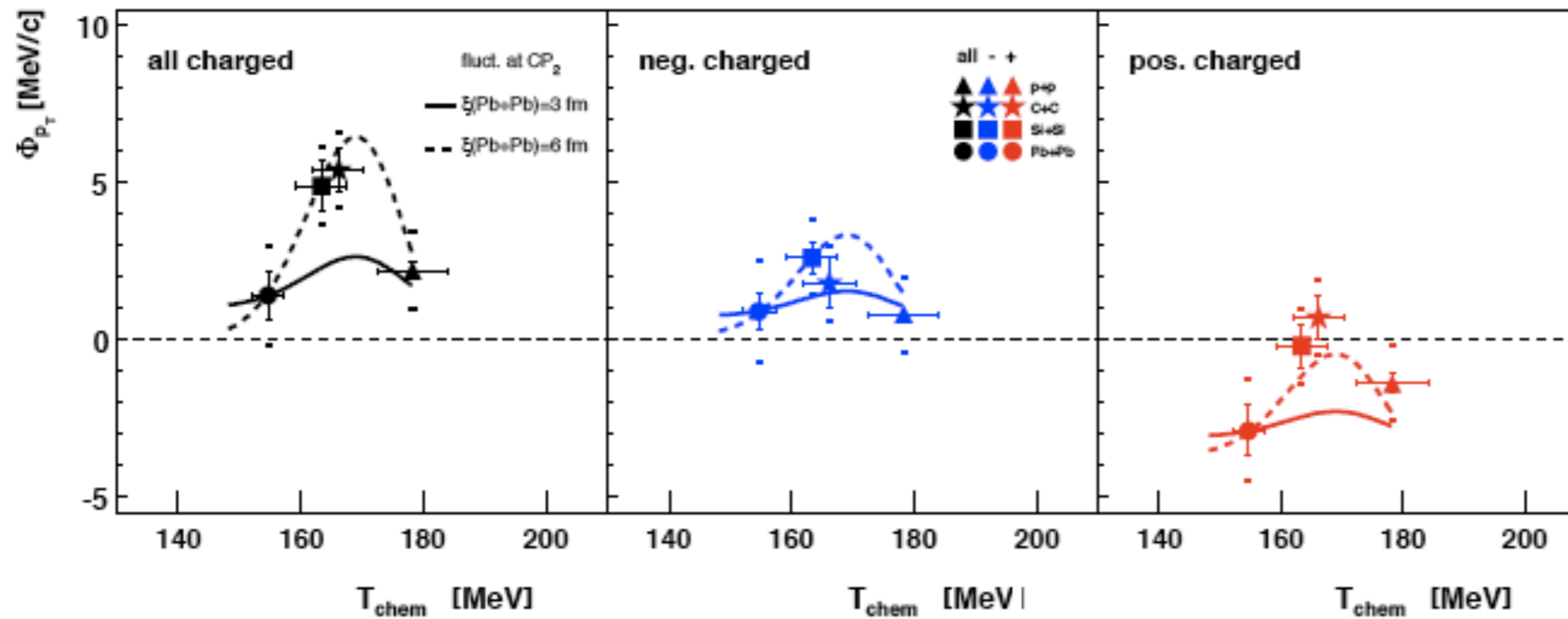


NA49 (2008)



$\langle p_T \rangle$  fluctuations<sup>(\*)</sup> at 1% level, independent of  $\sqrt{s}$

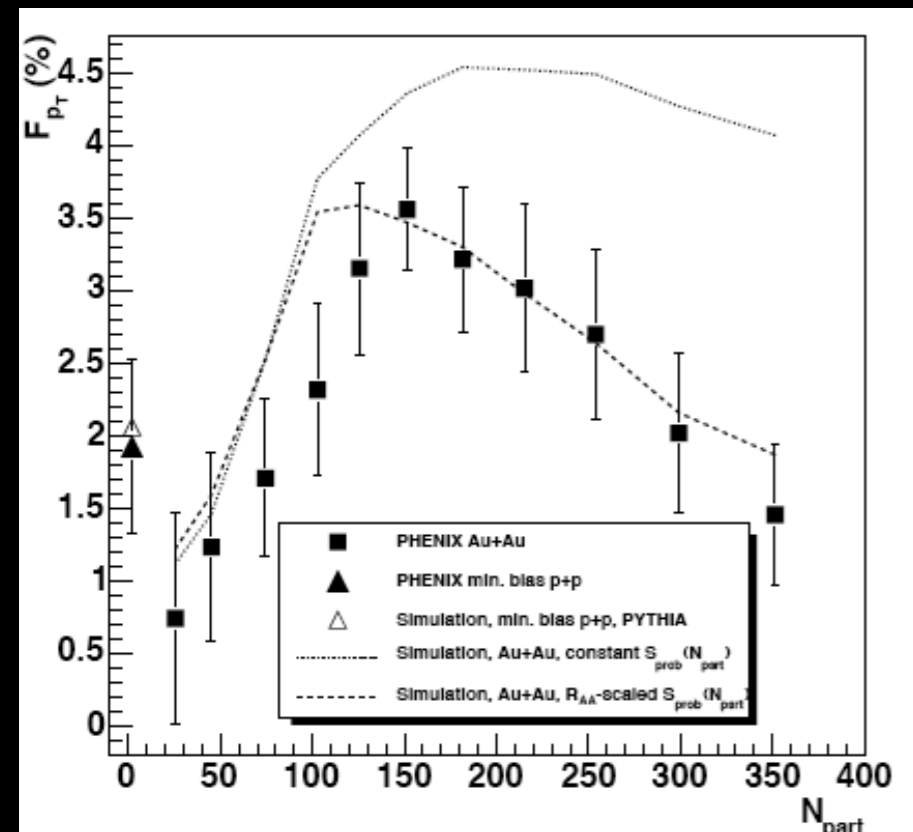
NA49/NA61 (2008)



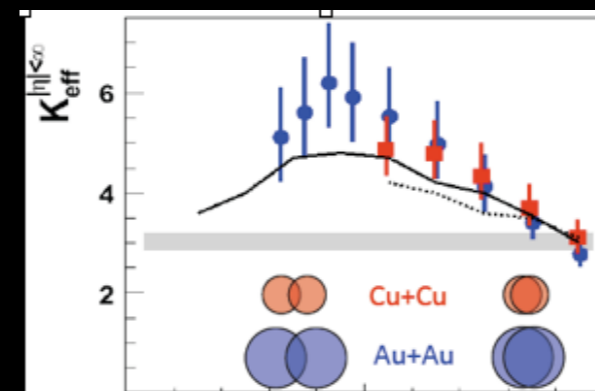
System size scan  
( $\sqrt{s} = 17.2$  GeV)

Rise and Fall vs system size is a ubiquitous feature of fluctuation/correlation observables

Interplay of two opposing trends  
(e.g. initial state fluctuations vs thermalization)

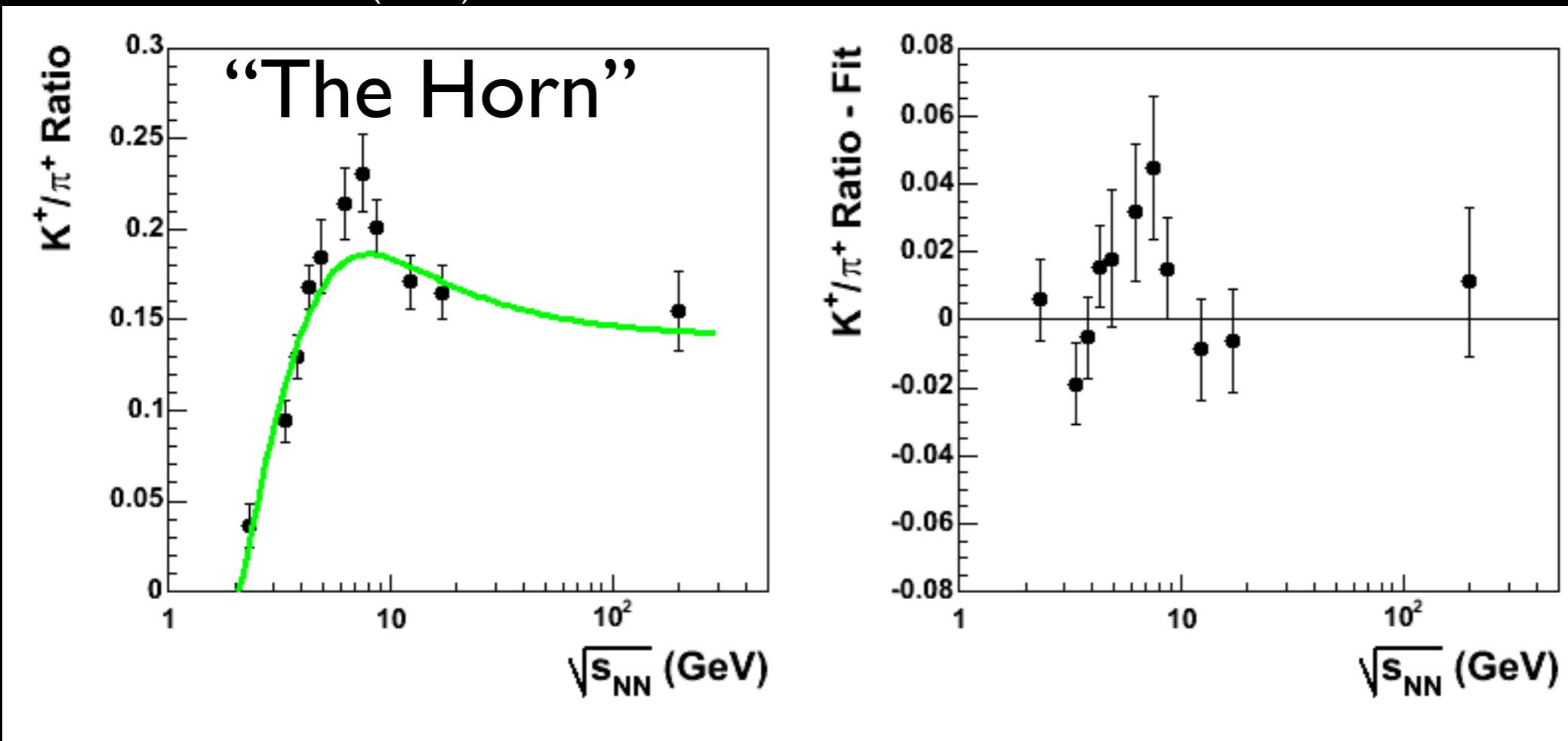


PHENIX (2003)

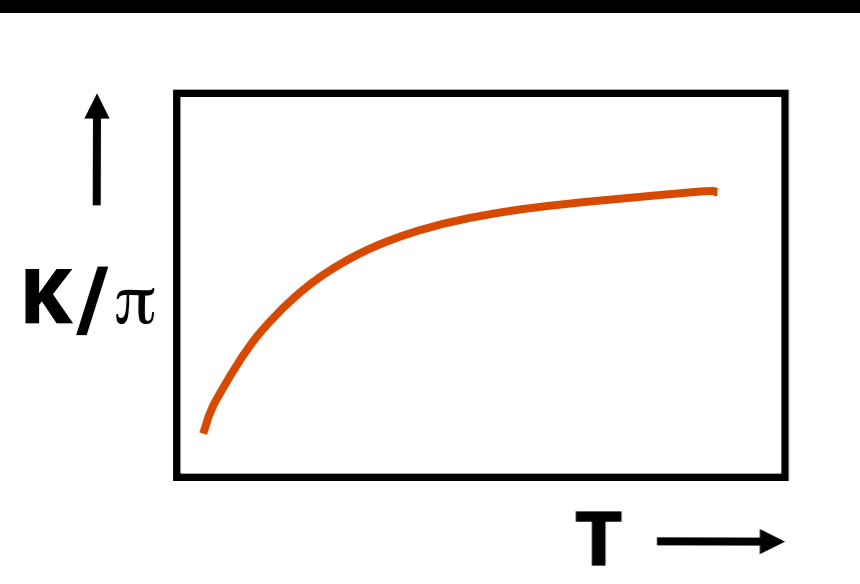




NA49 (2002)



Rapid change of  $\sqrt{s}$  dependence for  $k/\pi$  ratio



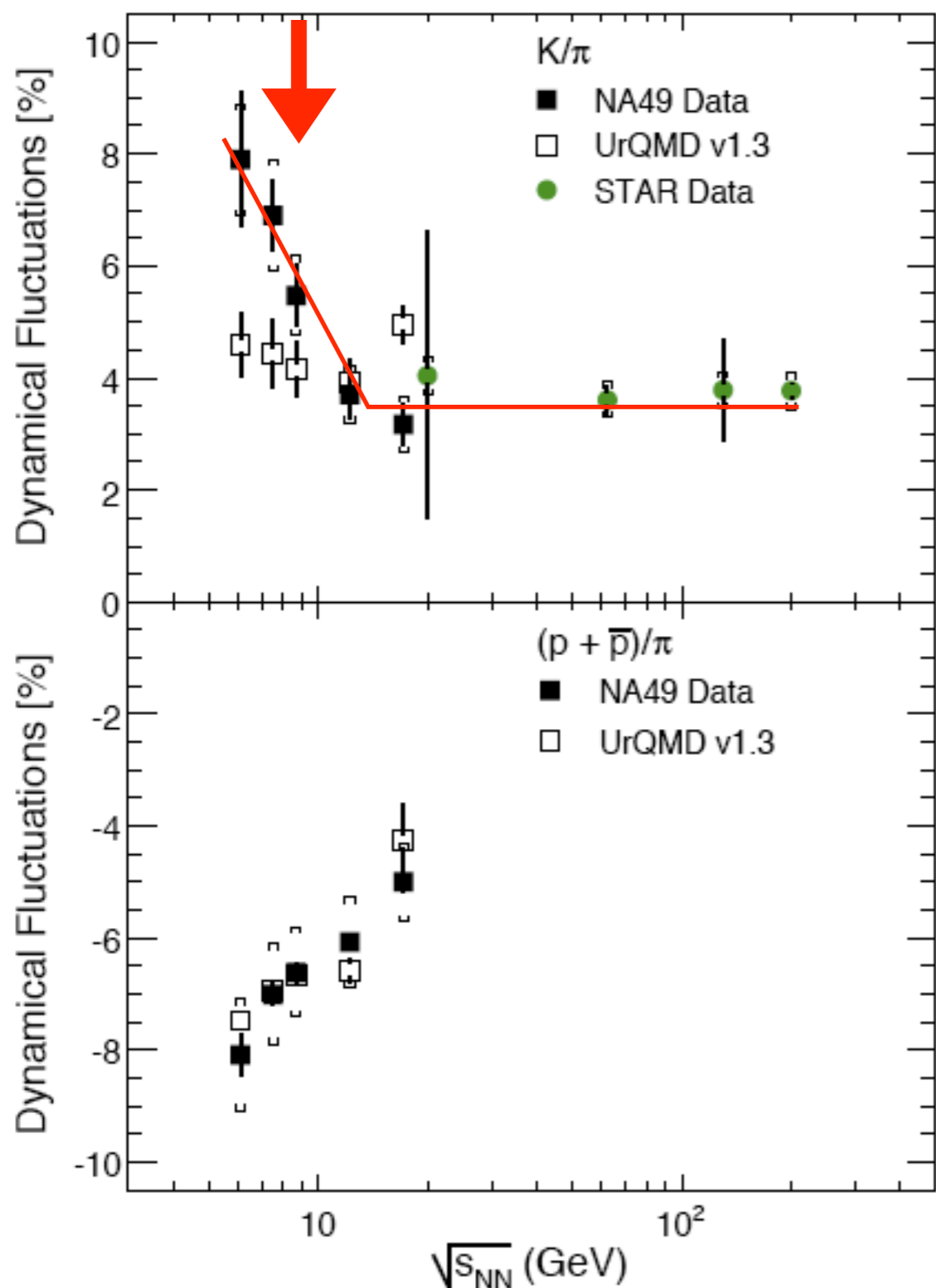
Obvious question: What happens with  $k/\pi$  fluctuations at  $\sqrt{s} \sim 8$  GeV?



# K/ $\pi$ fluctuations vs $\sqrt{s}$ in central PbPb



Horn

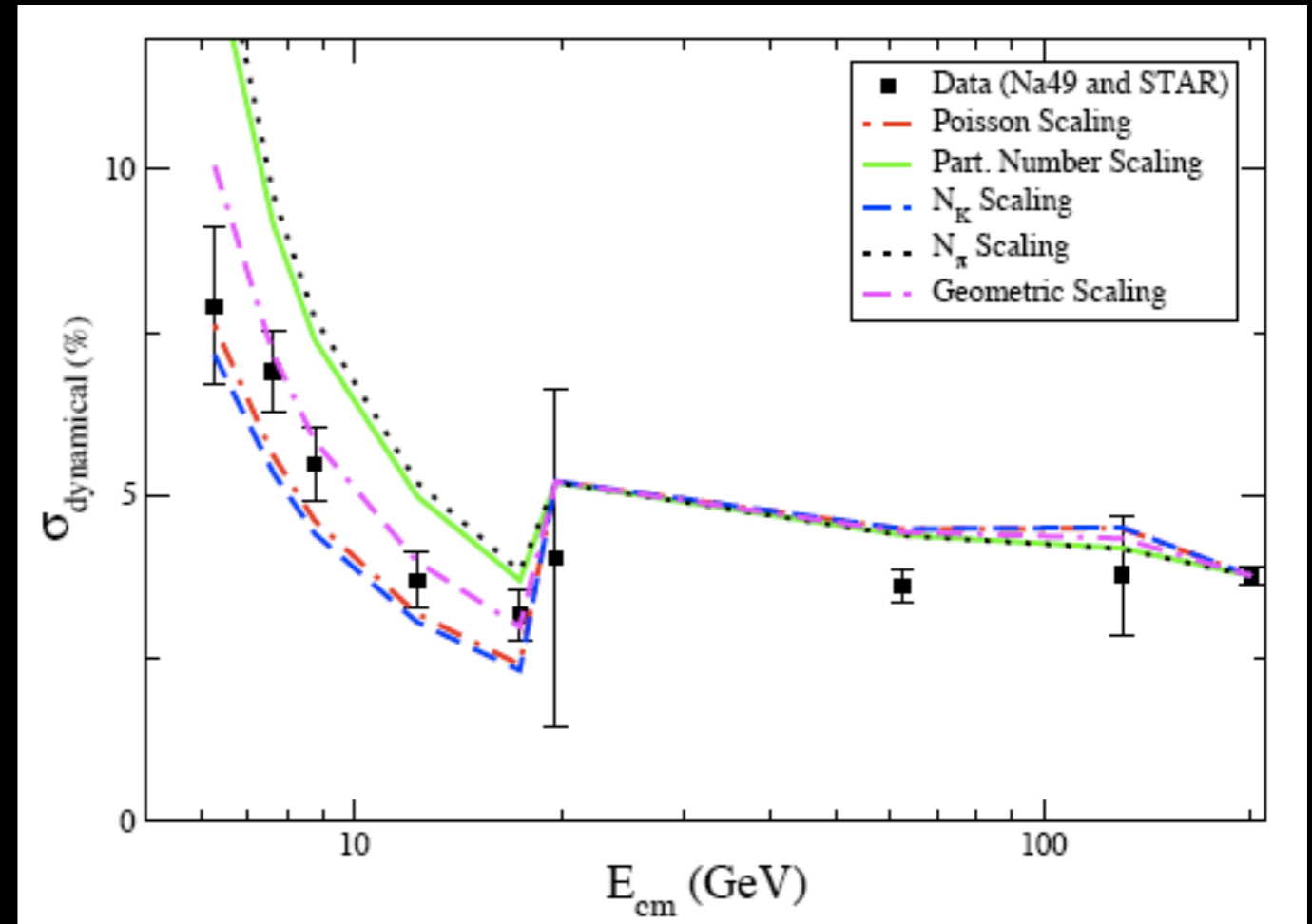
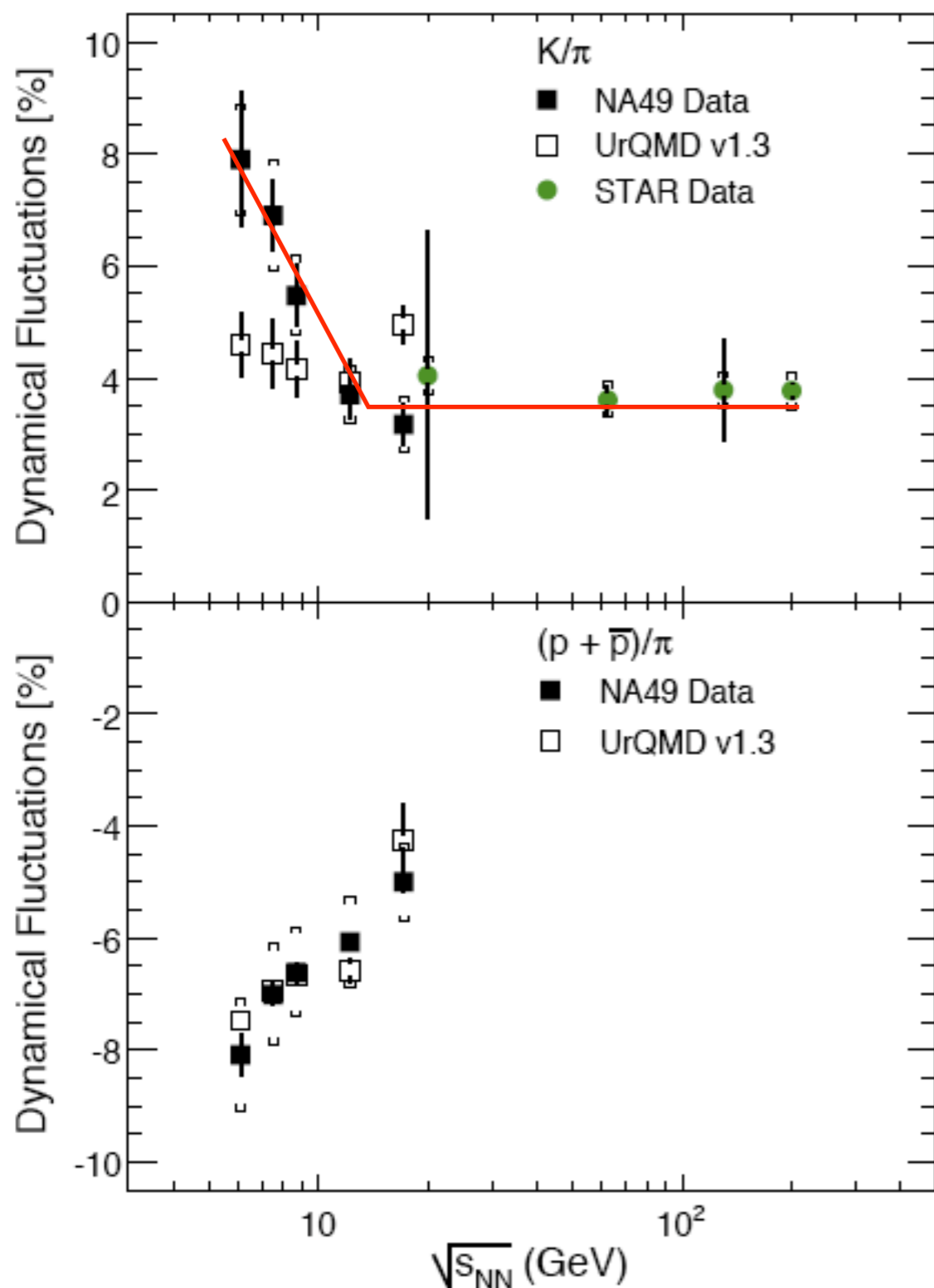


## Timeline

- 1994: NA49 first beam
- 1998: Preliminary result for  $\sqrt{s} = 17.2$  GeV
  - *Nucl.Phys.A638:91-102,1998*
- 2000: Final result for  $\sqrt{s} = 17.2$  GeV
  - *Phys.Rev.Lett.86:1965-1969,2001*
- 2004: Preliminary result  $\sqrt{s} = 5.5$  to 17.2 GeV
  - *J.Phys.G30:S1381-S1384,2004*
- 2008: Final result for PbPb vs  $\sqrt{s}$ 
  - *Phys.Rev.C79:044910,2009*

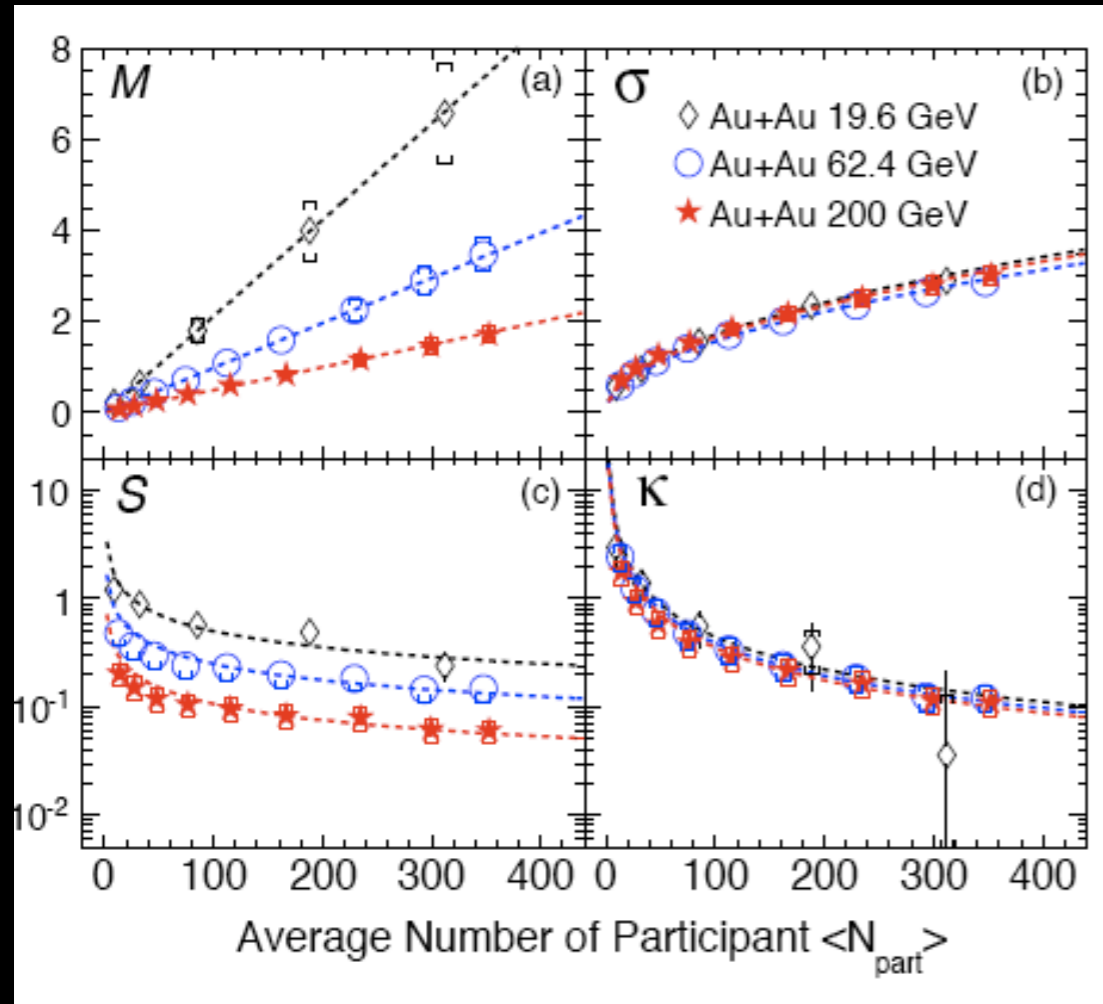
Strong, but monotonous,  
 $\sqrt{s}$  dependence of  
K/ $\pi$  fluctuations

Koch, Schuster (2009)

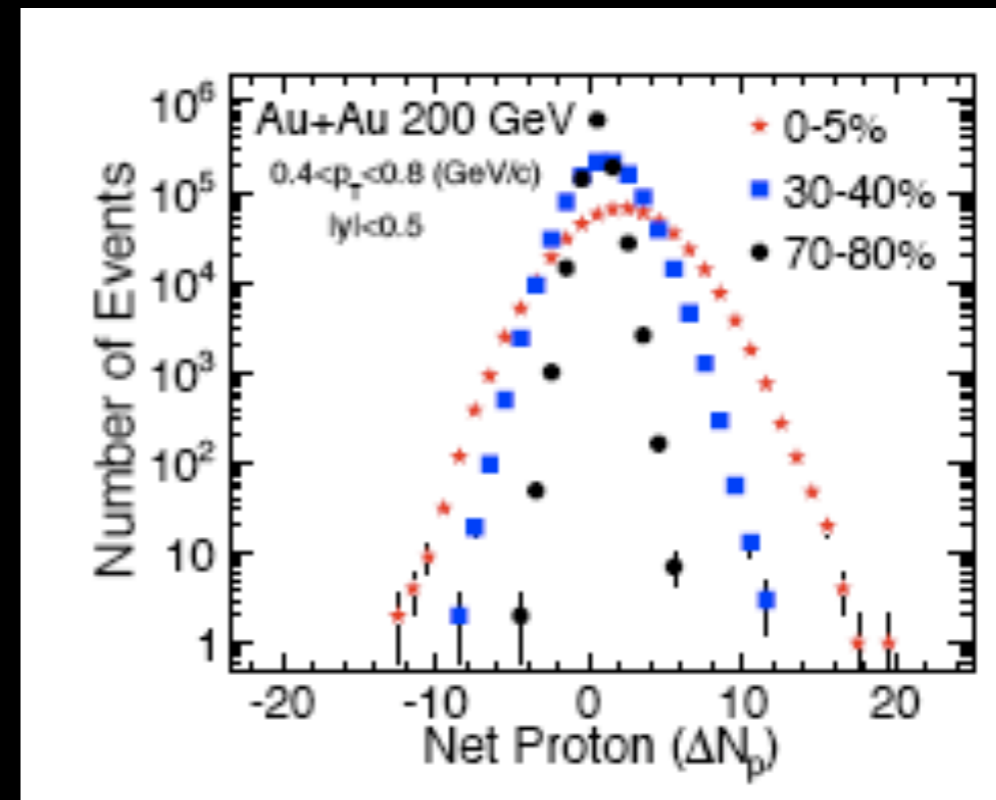


Data are compatible with constant correlation strength, once dilution with proper (i.e. in acceptance) multiplicity is taken into account

STAR (2010)



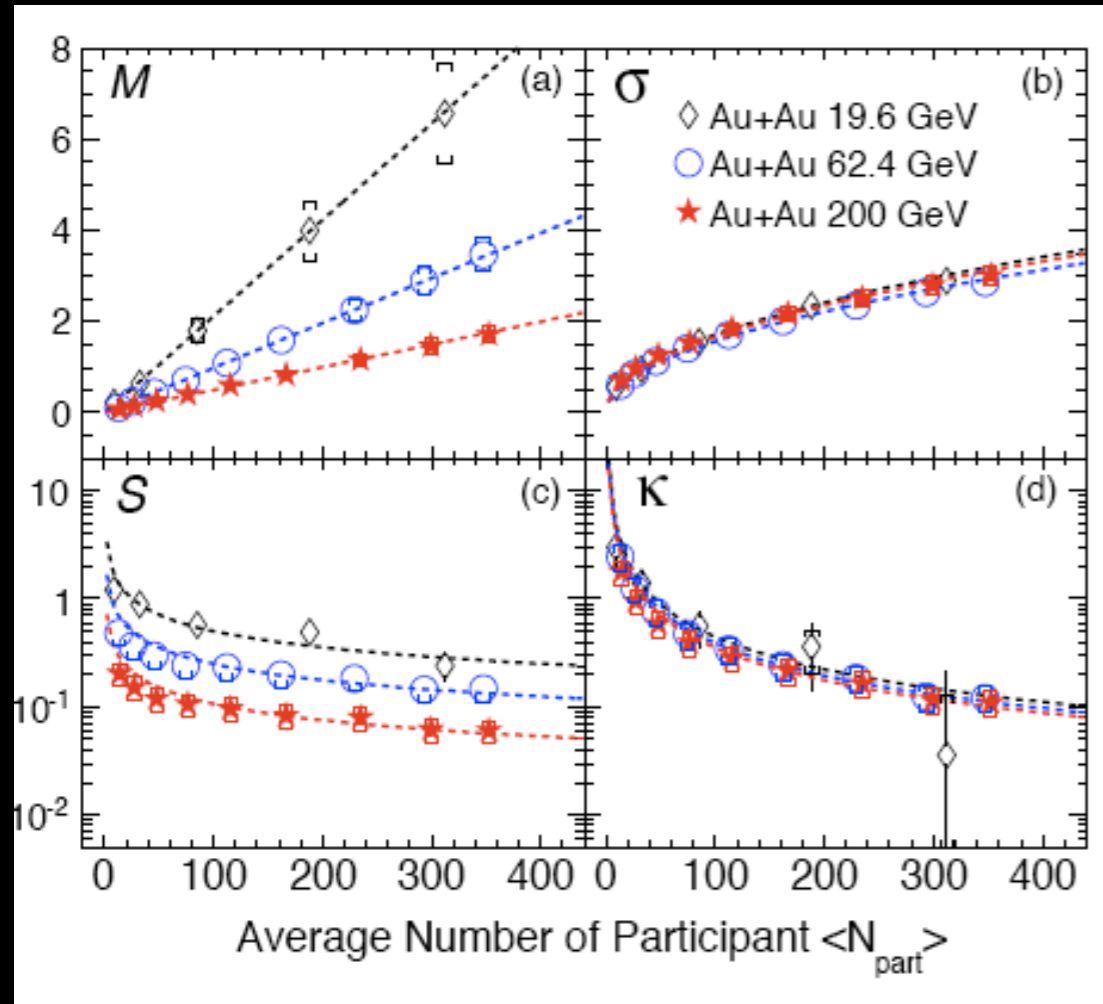
STAR (2010)



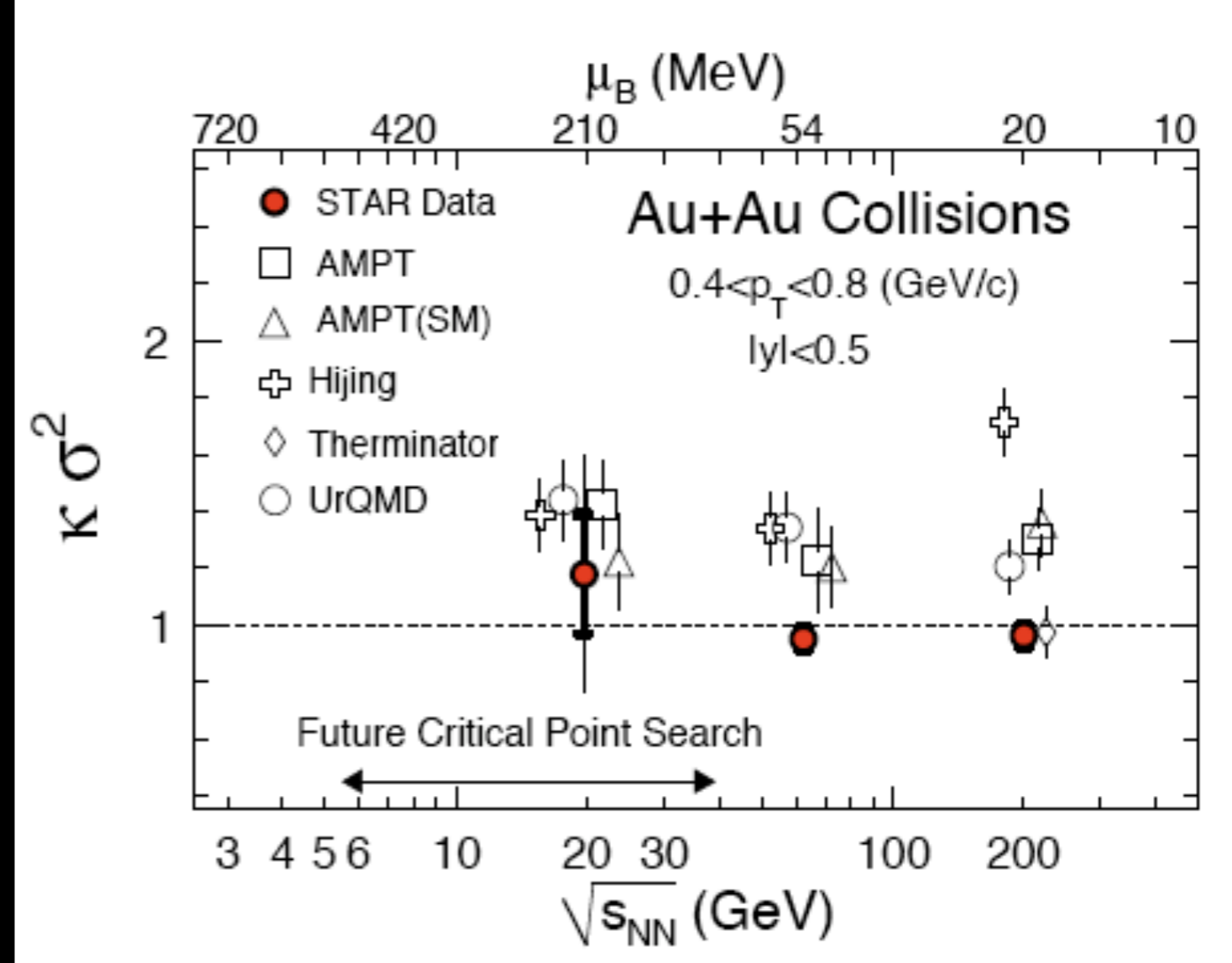
Moments of event-by-event net-baryon distributions are related to baryon number susceptibility

Experimentally, approximate net-baryons by net-protons

STAR (2010)



STAR (2010)



$$\kappa \sigma^2 = \frac{\chi_B^{(4)}}{\chi_B^{(2)} / T^2}$$

No sign of structure vs  $\sqrt{s}$  (yet)

Even less fluctuations than in models!?



- Fluctuations carry information about stages of the collision process
- Shape fluctuations are preserved in collision evolution
- Hadronization needs to be considered
- Still chasing the grand prize